

Hydrological Models and GRACE Satellite Observations in Cold Regions

by

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**Workshop Presentation
IP3 in Cold Regions**

Saskatoon, Oct 19-20, 2006

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Overview

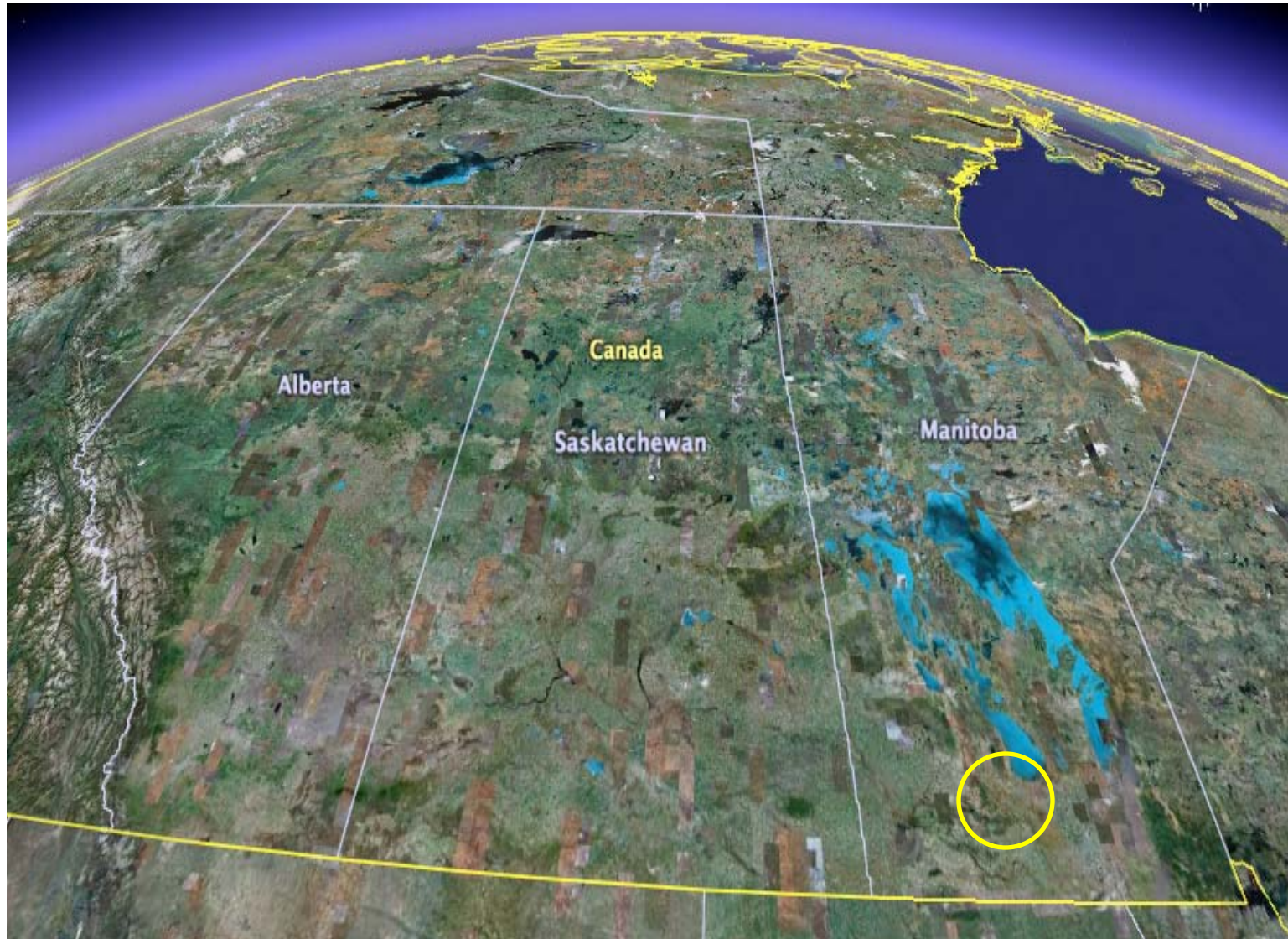
WatFLOW Development

- Adding groundwater for Atmospheric Models (CLASS)
- Coupling improved CLASS Model with Groundwater Model

GRACE Gravity Variation

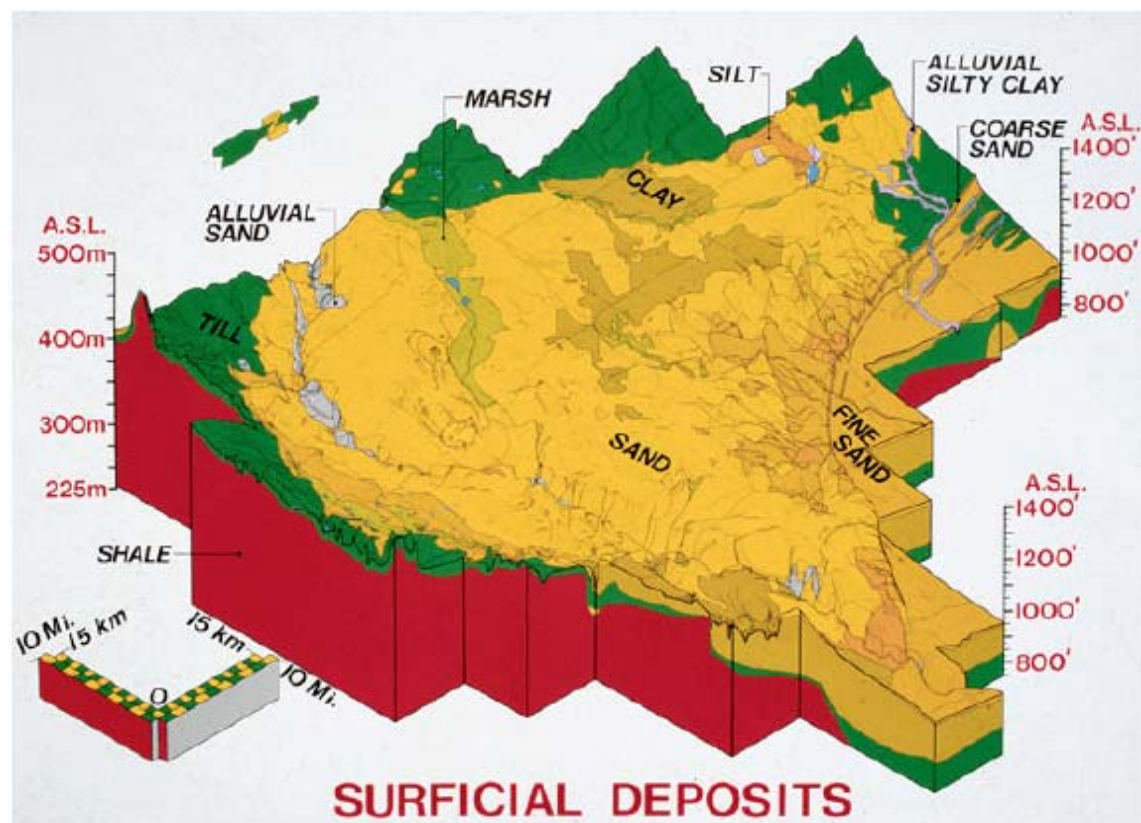
- Assess changes in moisture storage over Western Canada for Drought study
- Hydrological Model Calibration and Validation

Prairie Hydrology



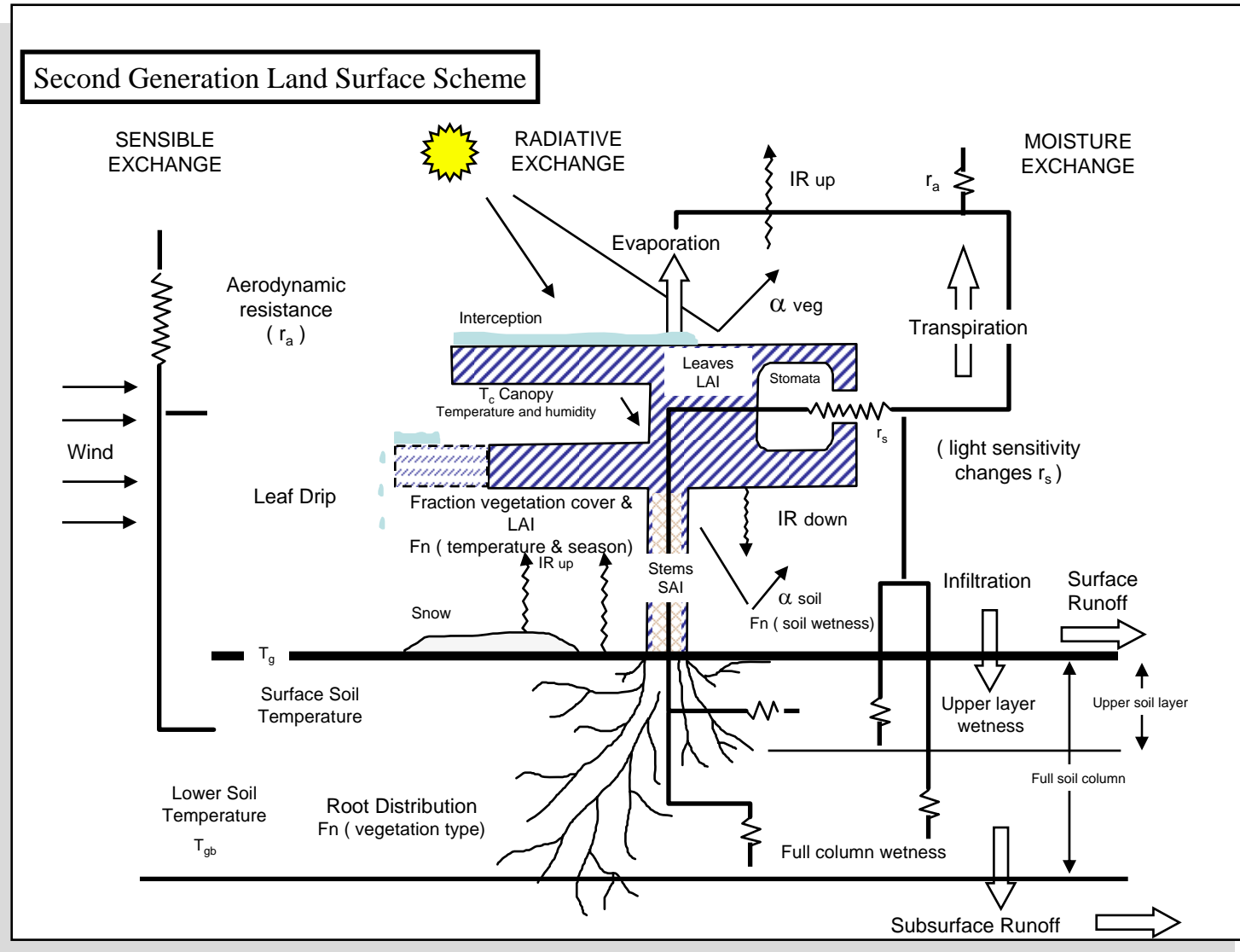
Assiniboine Delta Aquifer

Distribution of Surficial Deposits of the Assiniboine Delta Aquifer

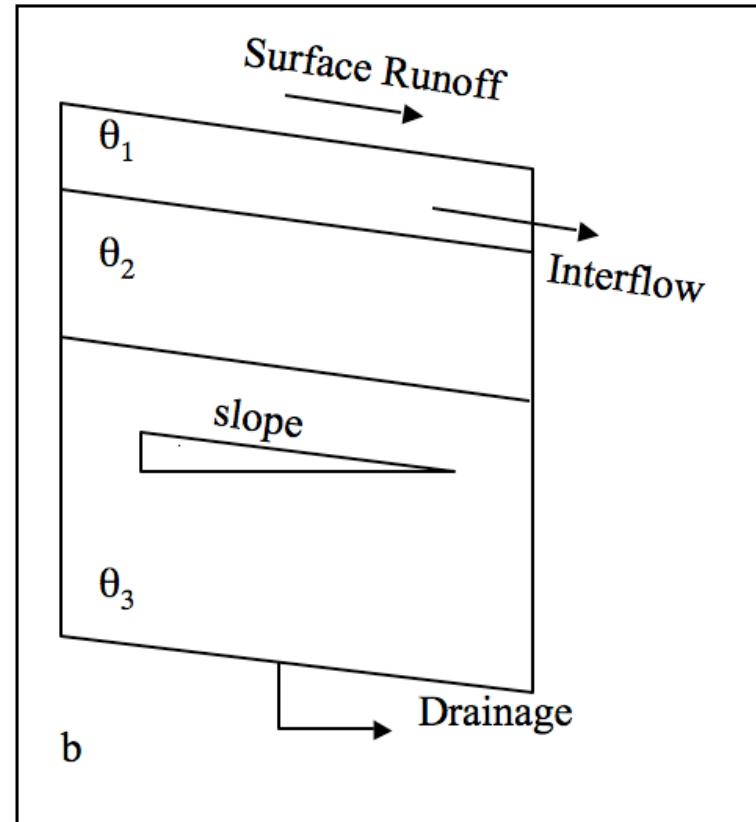
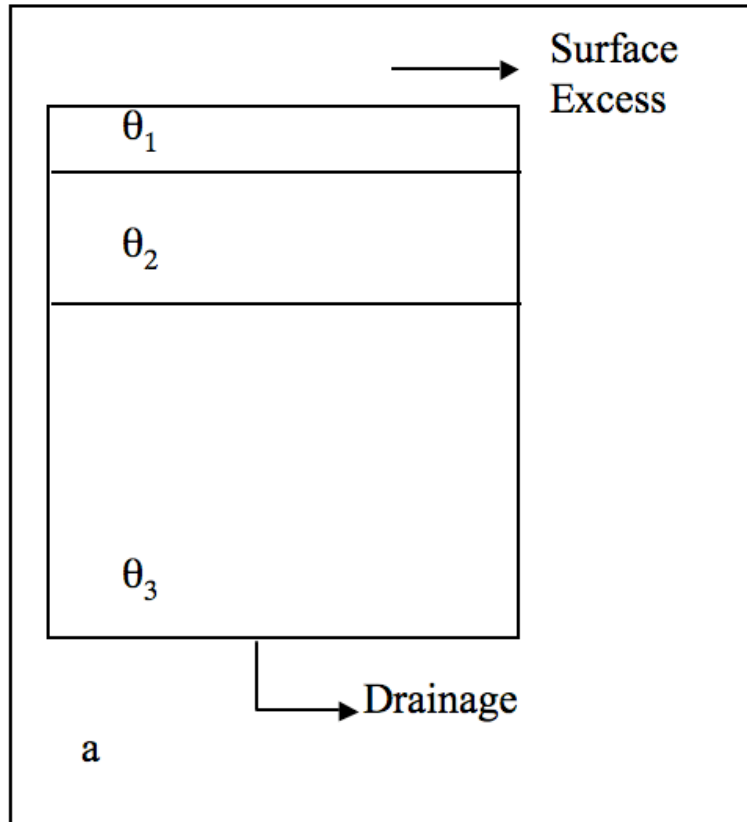


L.H. Frost and F.W. Render, 2002

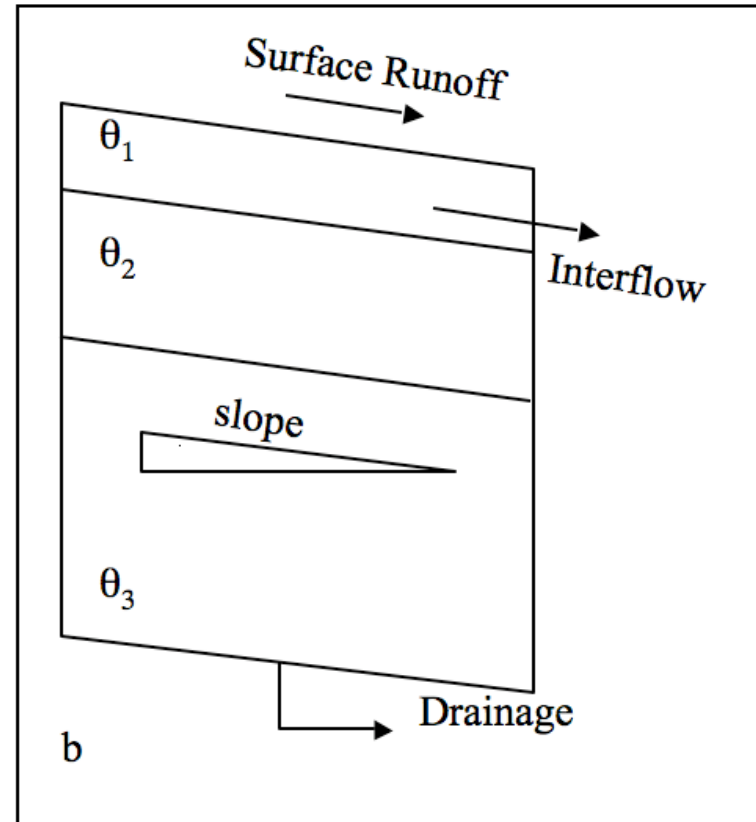
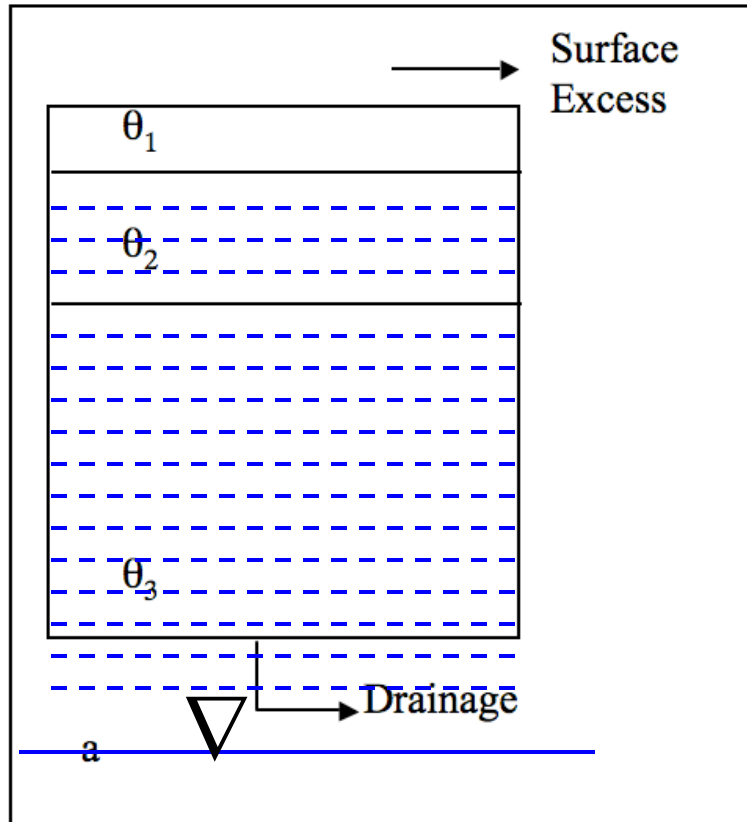
CLASS



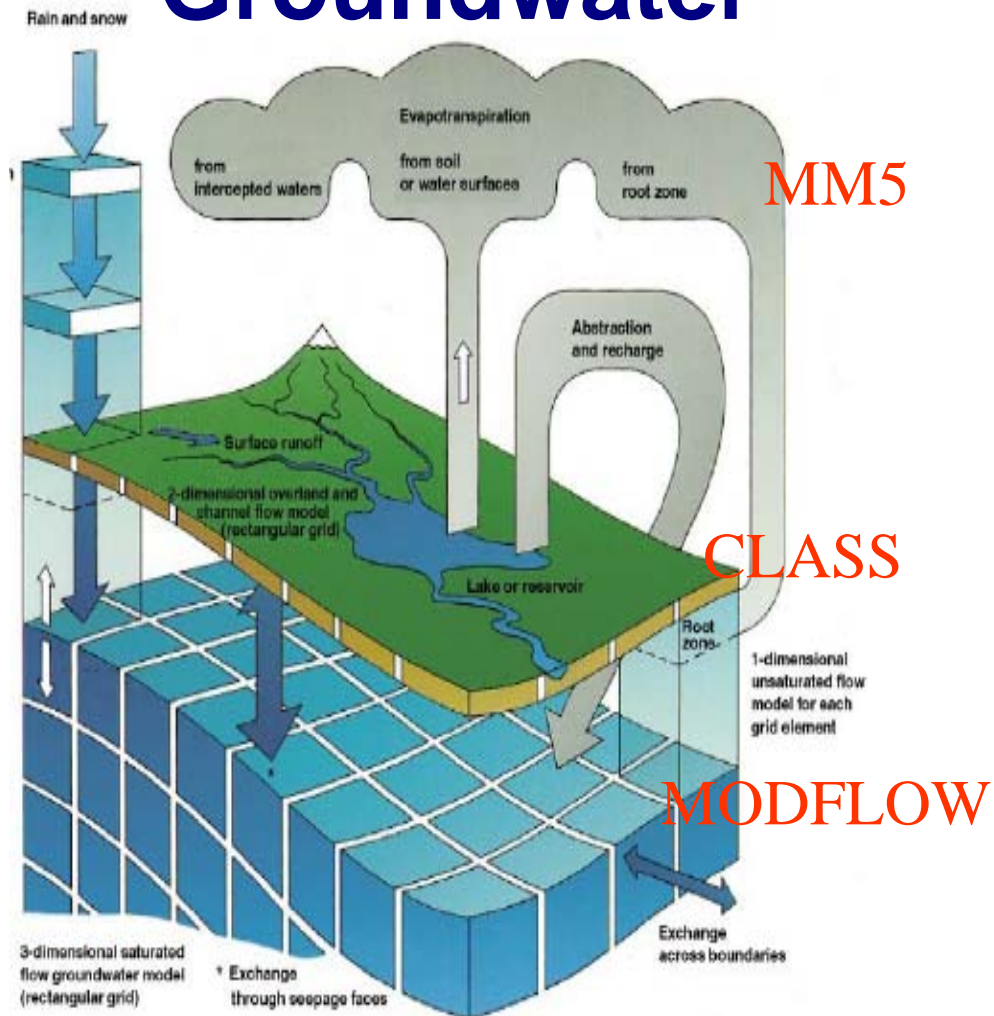
CLASS/WatCLASS



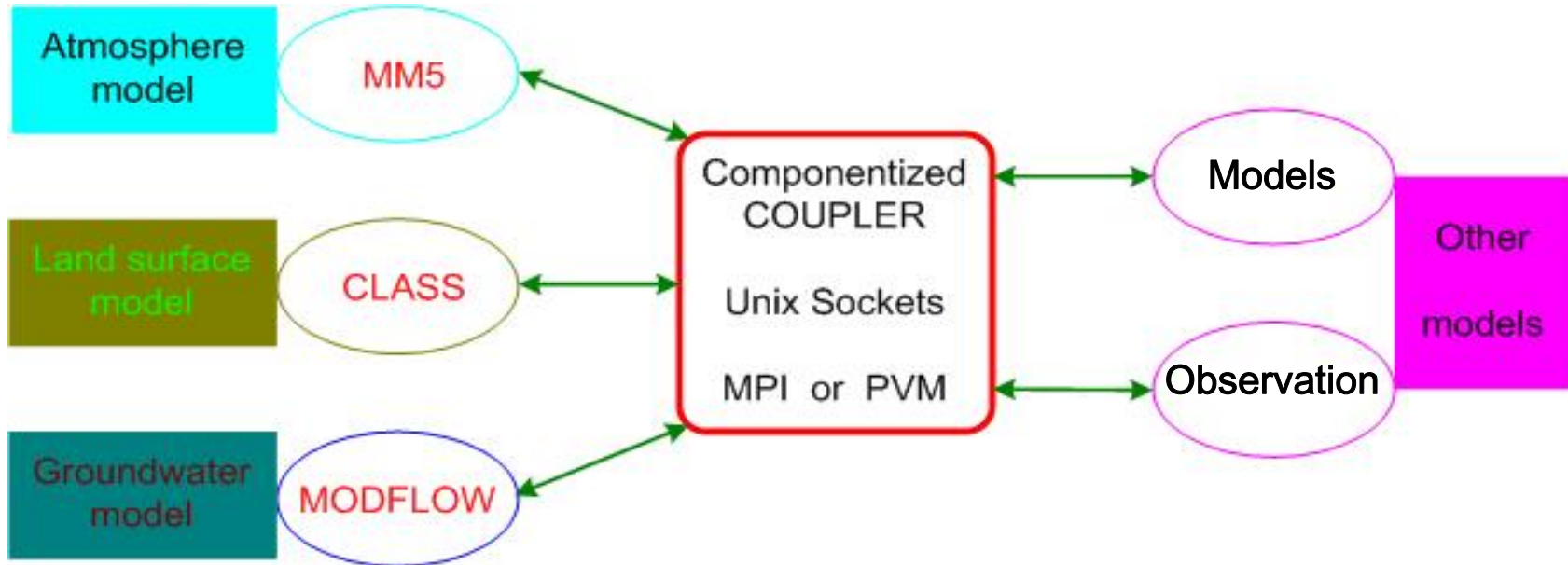
Coupling CLASS to Groundwater



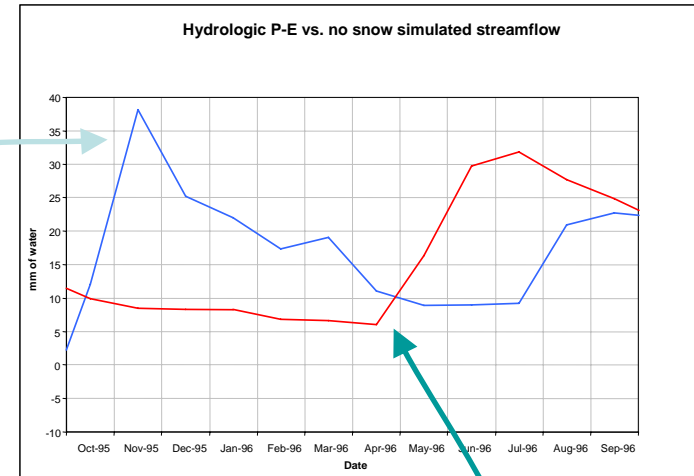
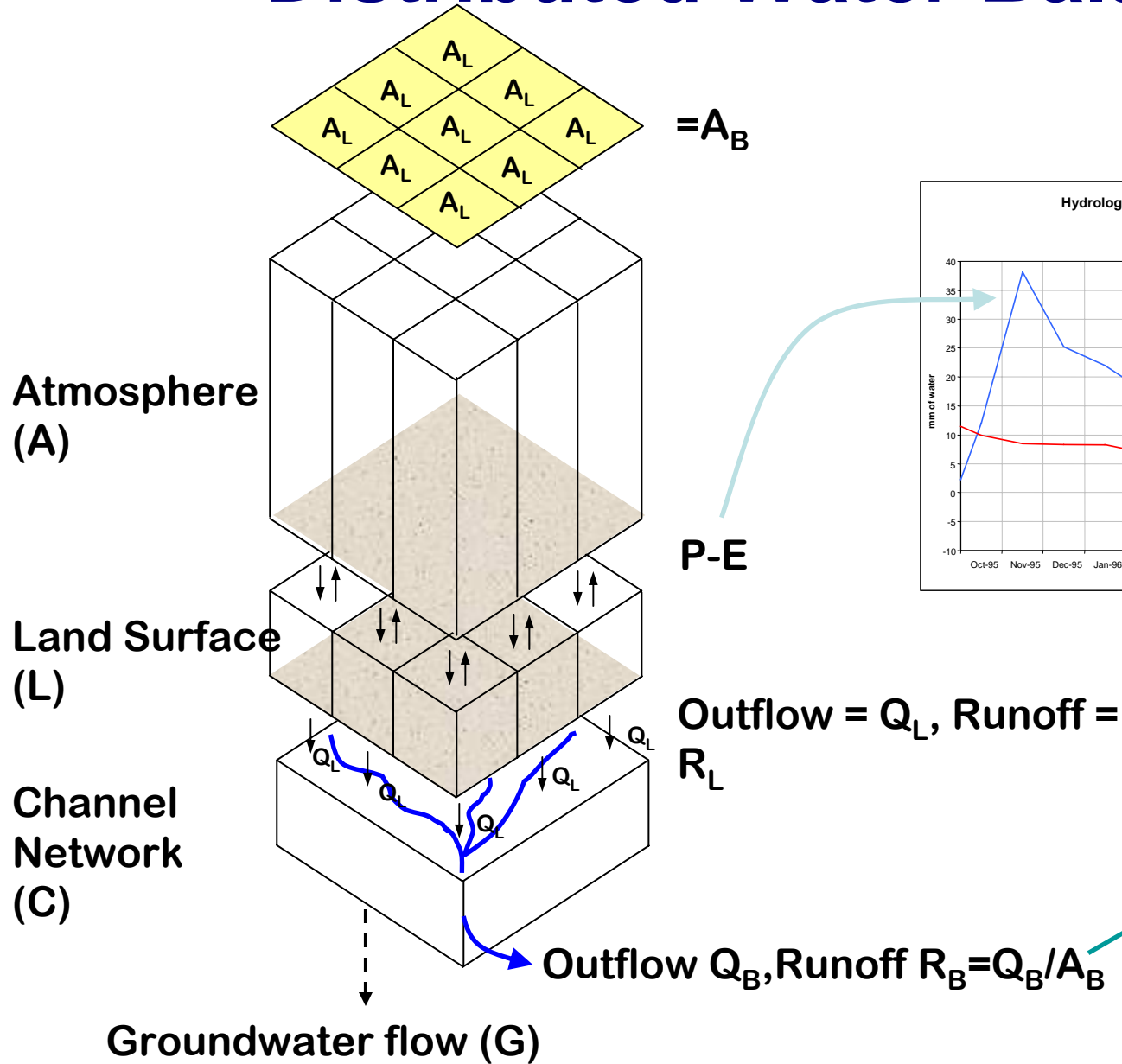
Coupling CLASS to Groundwater



Coupling CLASS to Groundwater



Distributed Water Balance



GRACE Terrestrial Moisture Changes

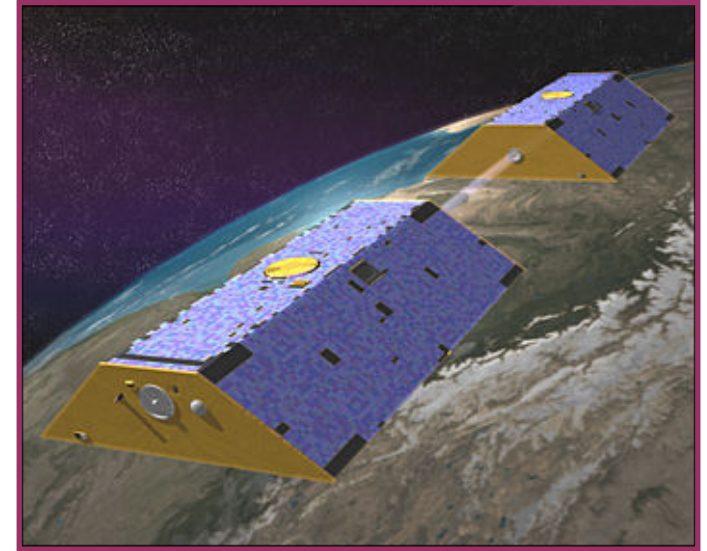
Introduction

Twin GRACE Satellites

Launch on 2002 March 17

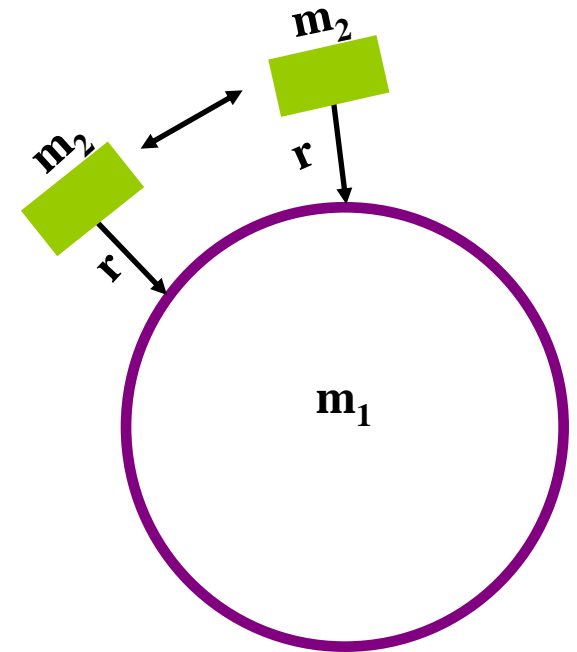
Flying approximately 220 km apart

Altitude of 400-500 km

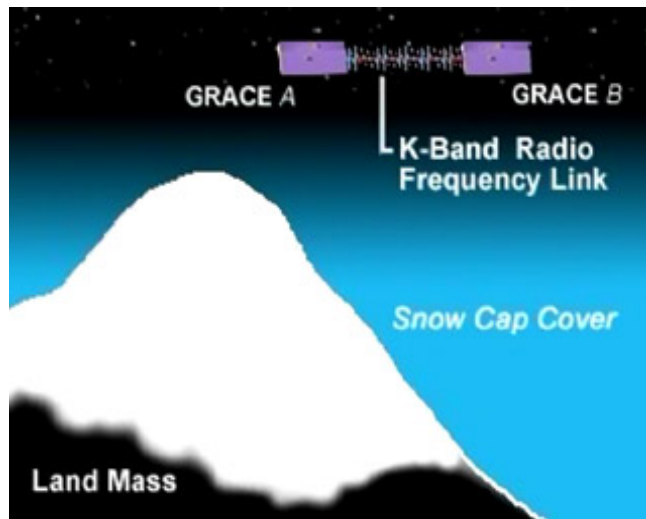


Newton's Law of Gravitation

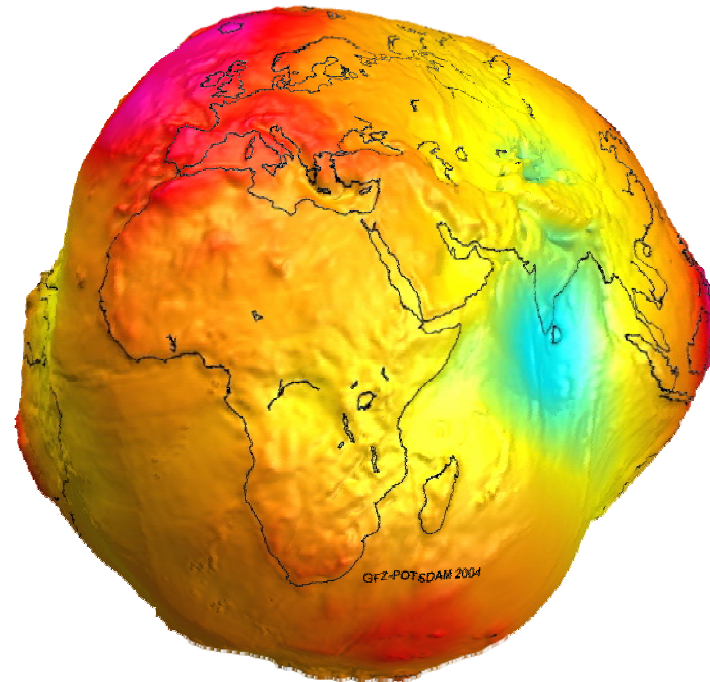
$$F = k \frac{m_1 m_2}{r^2}$$



GRACE Primary Mission



Gravity Model



- Develop geoid from averages over 5 year life
- Monthly variations related to surface moisture changes

Creation of Earth Geopotential Map

Time-variable geopotential $\delta G(t)$ solution of Laplace Equation

$$\delta G(t) = \sum_{n=1}^N \sum_{m=0}^n (\delta C_{nm}(t) \cos m\lambda + \delta S_{nm}(t) \sin m\lambda) P_{nm}(\cos \theta)$$

where:

θ is the latitude

λ is the longitude

m & n are harmonic degree and order

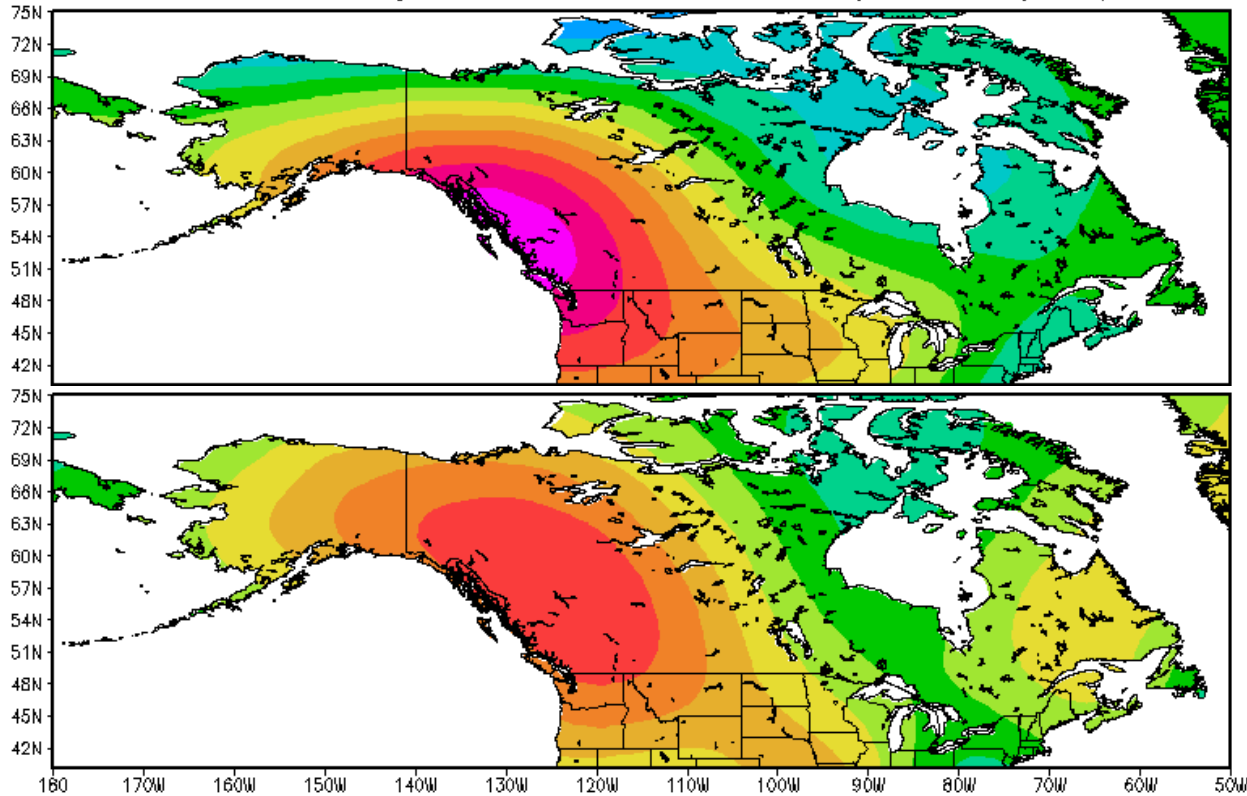
P is Legendre's polynomial

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FIRST GAA-2_0020_2002306-2002334_EIGEN_G---_0001 SHM GFZ POTSDAM 20040202
CMNVT non-tidal atmosphere geopotential coefficients averaged over certain time period
EARTH 0.3986005000E+15 0.6378137000E+07
SHM 100 100 0.00 fully normalized not applicable
GRCOF2 0 0 -0.318825125047E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 1 0 -0.743858323766E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 1 1 0.467836111096E-10 0.201460491997E-09 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 2 0 -0.141179449975E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 2 1 0.435618459063E-10 0.146290536678E-09 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 2 2 -0.633075610331E-10 0.406058075398E-11 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 3 0 -0.736090450659E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 3 1 -0.199073761293E-10 0.232869076584E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 3 2 -0.490601878460E-10 -0.180914669352E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 3 3 0.233728051297E-10 0.252474471129E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 4 0 0.772325111156E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 4 1 0.487204463462E-12 0.666863217404E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 4 2 -0.727619399319E-10 0.276098411436E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 4 3 -0.193220833088E-10 0.750166278890E-11 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 4 4 0.151414277145E-10 -0.248385690333E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 5 0 0.337665842182E-10 0.000000000000E+00 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 5 1 -0.251601443547E-10 0.201935048512E-10 0.0000E+00 0.0000E+00 021102.080000
GRCOF2 5 2 -0.297940386111E-10 -0.146666550122E-10 0.0000E+00 0.0000E+00 021102.080000
    
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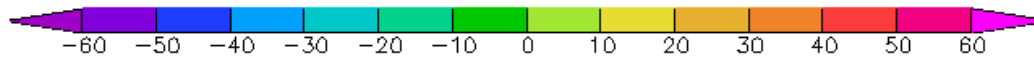
Monthly Difference Result

Water Storage relative to mean Geopotential(mm)



April 2002

April 2003



mm of Equivalent water thickness

Water Balance Methods

Atmospheric Moisture Budget:

$$\langle P - E \rangle_a = - \langle \partial q / \partial t \rangle - \langle \nabla \cdot \mathbf{Q} \rangle$$

Where: (P-E) = difference between precipitation and evapotranspiration,
q = the vertically-integrated vapour mass or precipitable water,
 $\nabla \cdot \mathbf{Q}$ = the moisture flux divergence,
Q = qV ; V is wind speed

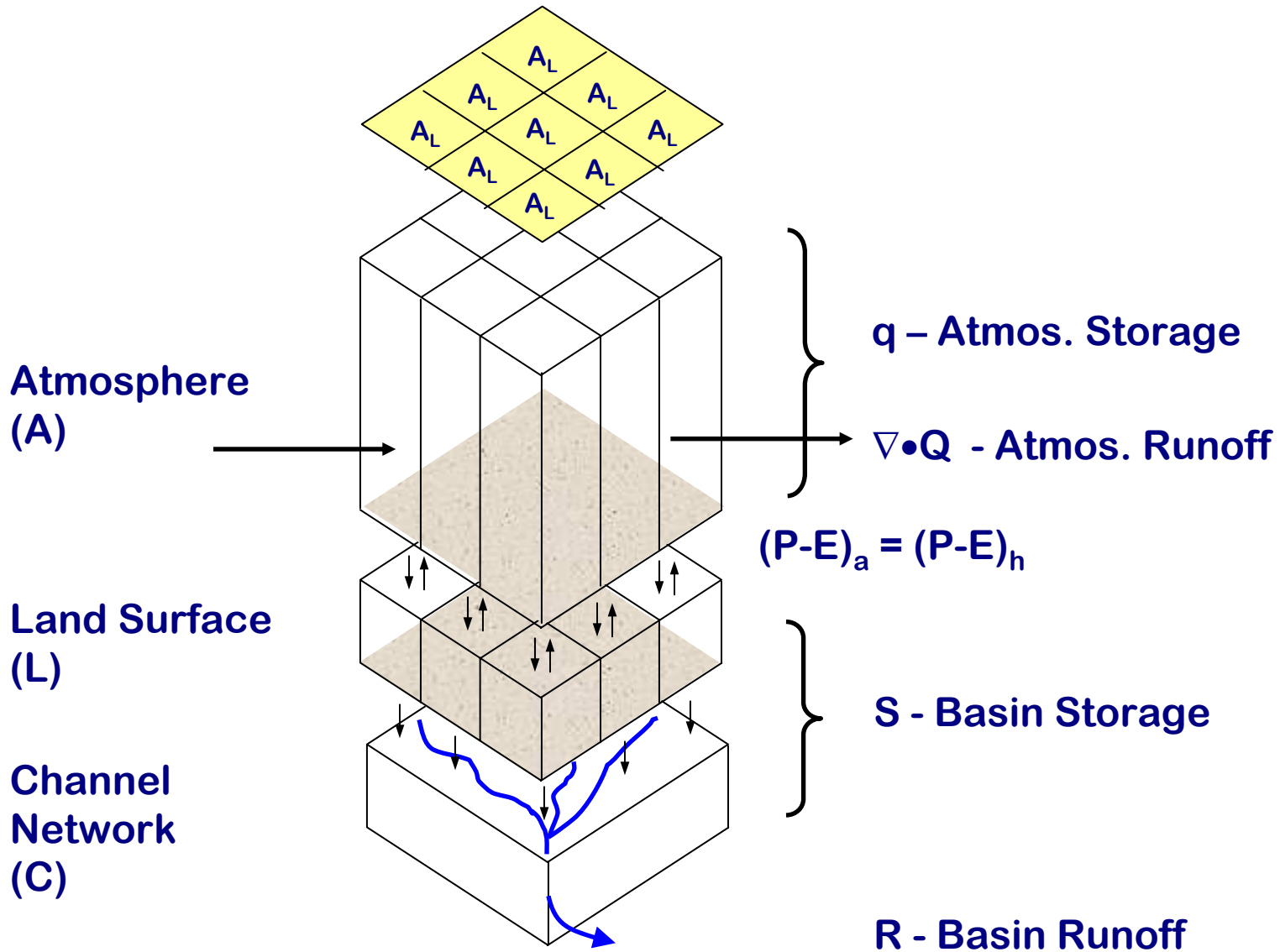
Hydrologic Water Budget:

$$\langle P - E \rangle_h = \langle R \rangle + \langle \partial S / \partial t \rangle$$

where: S = surface water storage
R = basin runoff

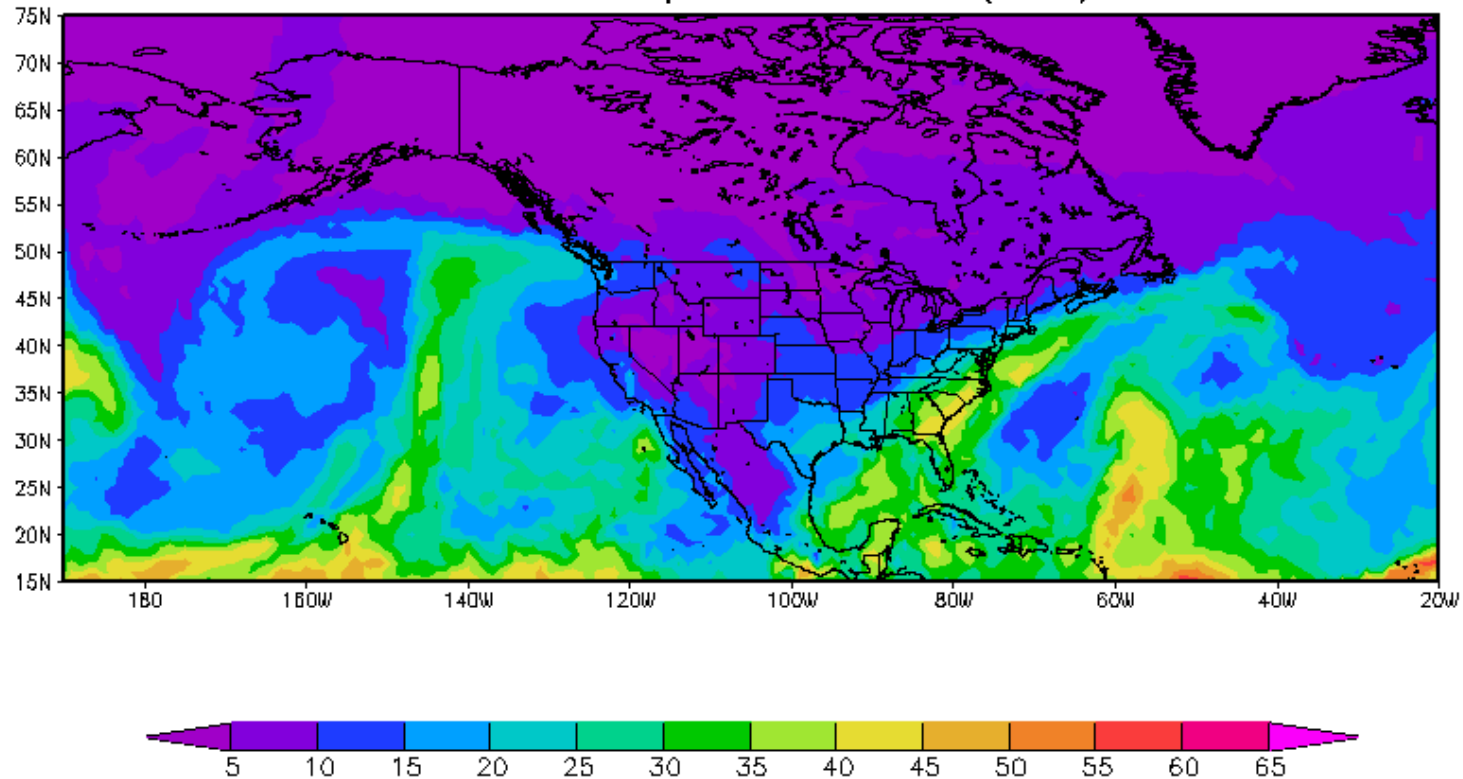
$$\text{Grace Result} := \langle \partial S / \partial t \rangle + \langle \partial q / \partial t \rangle$$

Water Balance Methods



q - Atmospheric Storage

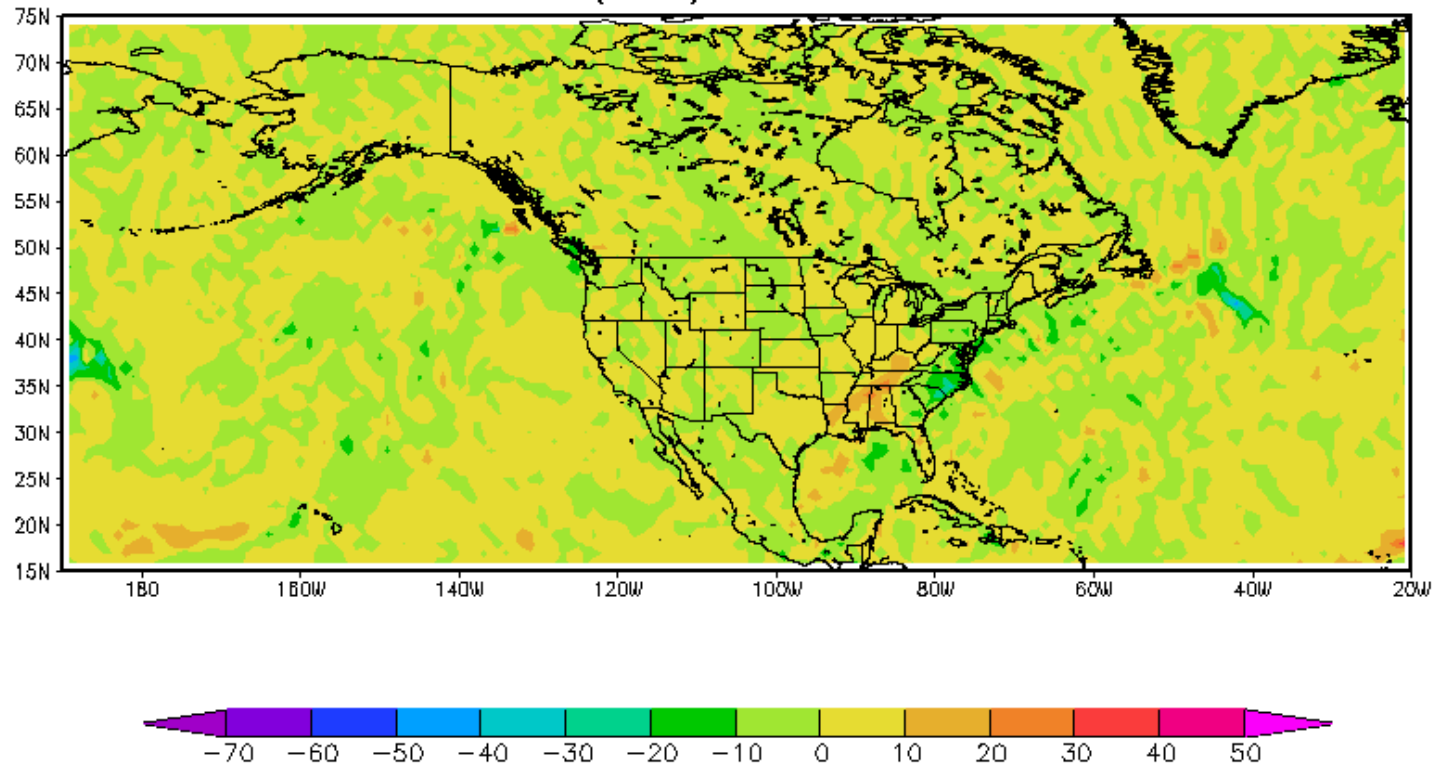
water content in the atmospheric column(mm) 00Z01APR2002



Data Source: CMC 4x Daily Analysis

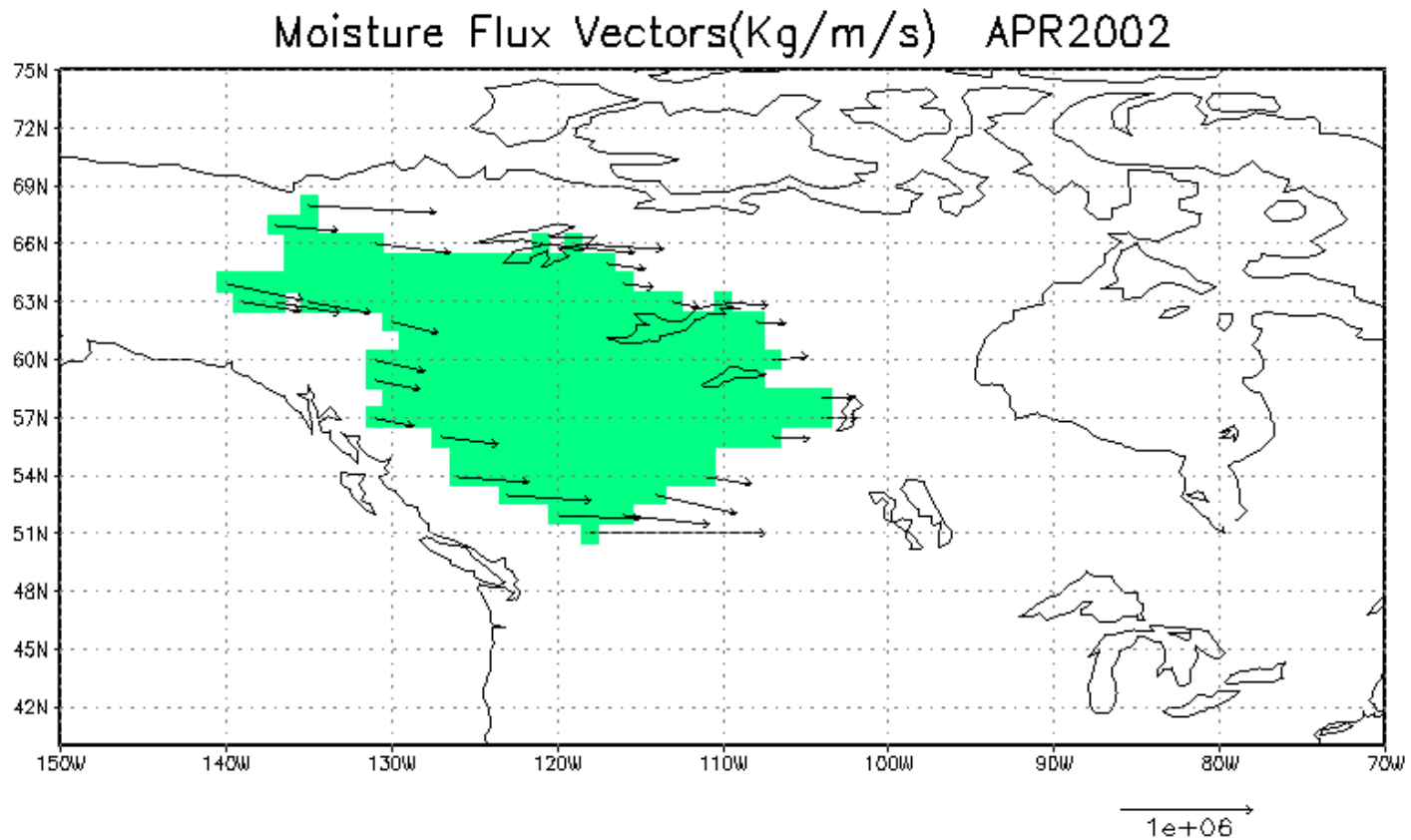
$\nabla \cdot Q$ - Atmospheric Runoff

Net flux(mm) 00Z01APR2002



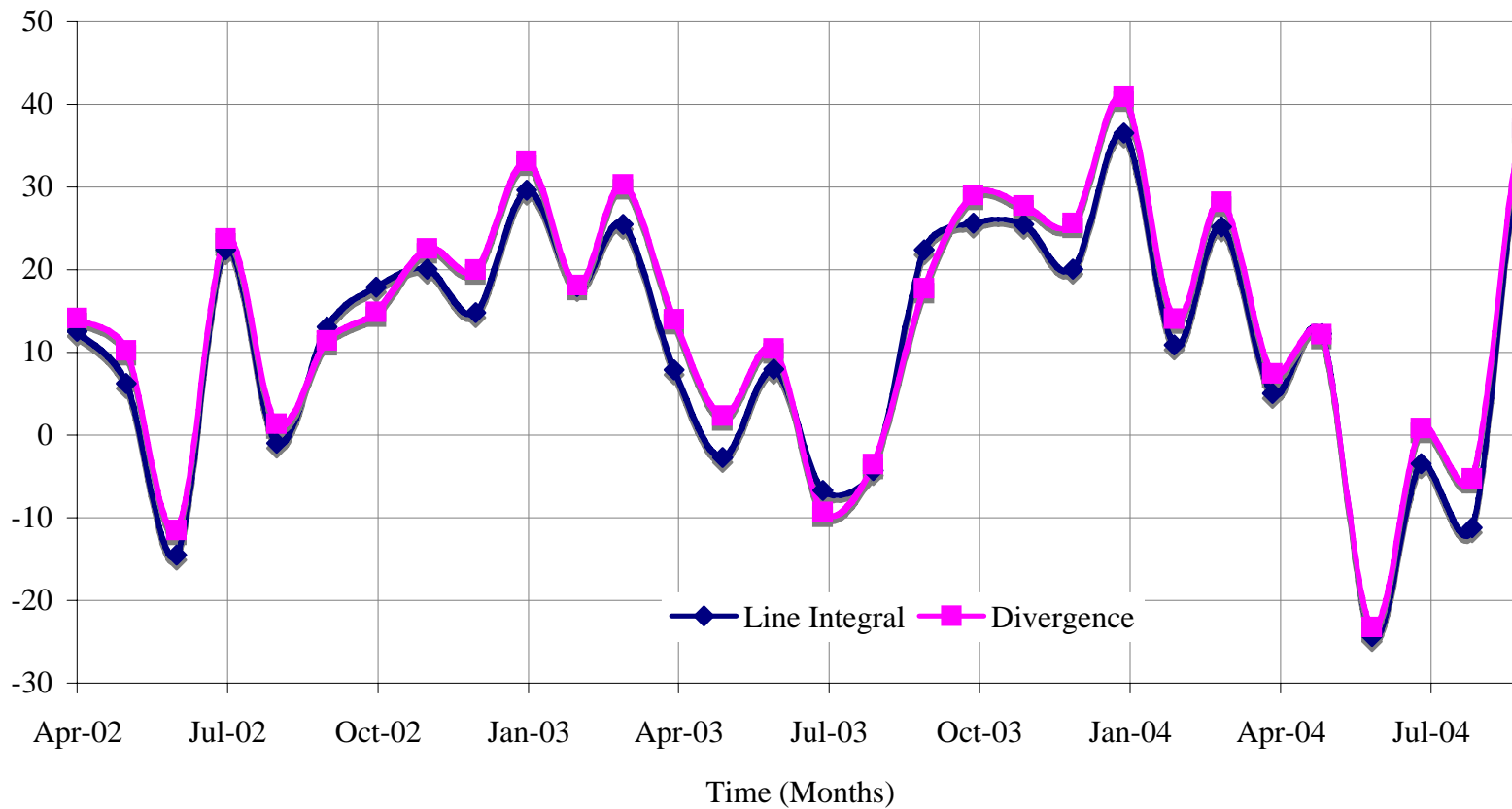
Data Source: CMC 4x Daily Analysis

Alternate $\nabla \cdot \mathbf{Q}$ - Calculation

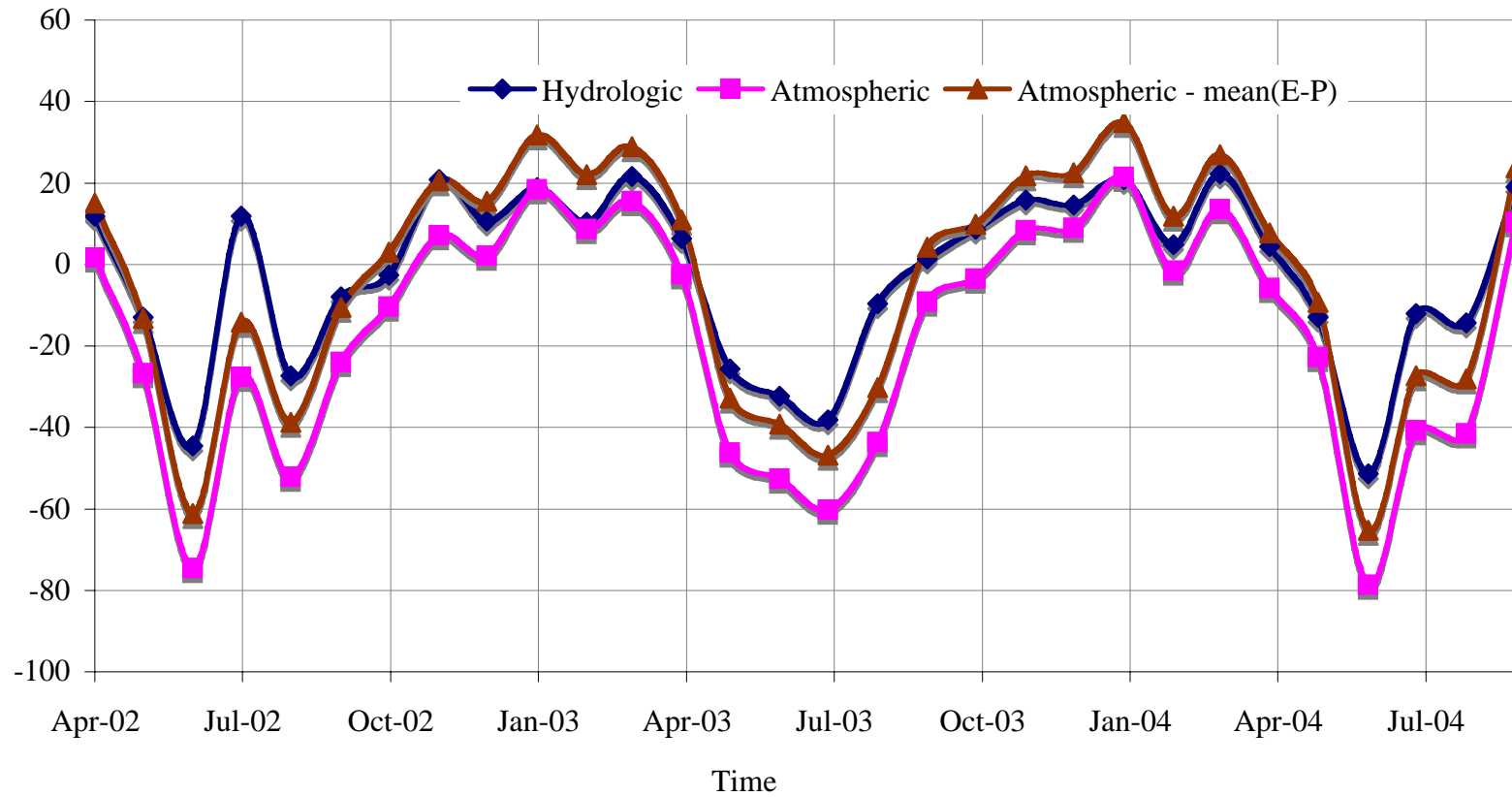


via Green's Theorem

Atmospheric (P-E) For Water Years 2002-2004 (Mackenzie River Basin)



Atmospheric and Hydrologic Basin Change in Storage For Water Years 2002-2004 (Mackenzie River Basin)



Atmospheric, Hydrologic and GRACE based Change in Storage relative to mean Geopotential For Water Years 2002-2004 (Mackenzie River Basin)

