



# Hydrological Processes and Parameterization: Infiltration and Runoff

Sean K. Carey, Yinsuo Zhang, Jessica Boucher, Michael Treberg,  
Bill Quinton, Ric Janowicz,

Dept. Geography & Environmental Studies  
Carleton University, Ottawa



- **Runoff**
  - Ecosystem Controls
  - Transit Time Distributions
  - Channel Snow/Ice
  
- **Infiltration**
  - Parameterization/modelling activities
  
- **HRU Classification**



# The Wolf Creek Research Basin



Location:  
60°31' N, 135° 31' W

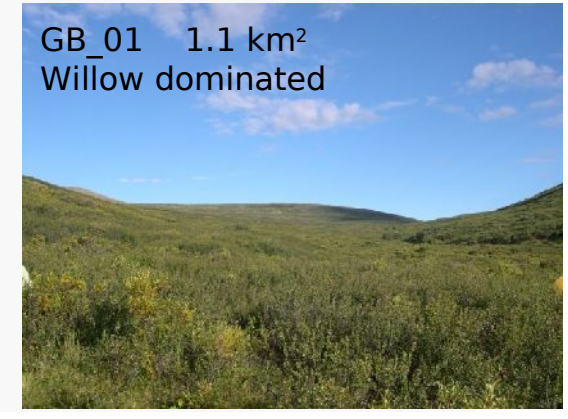
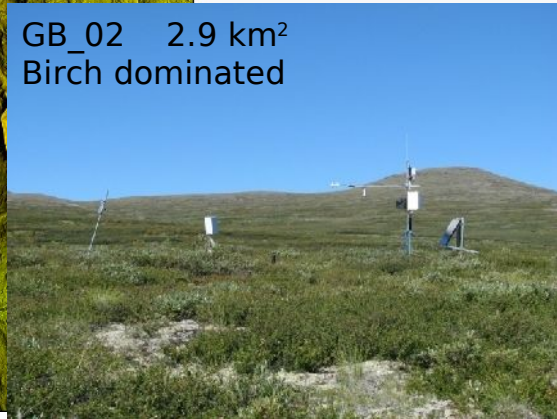
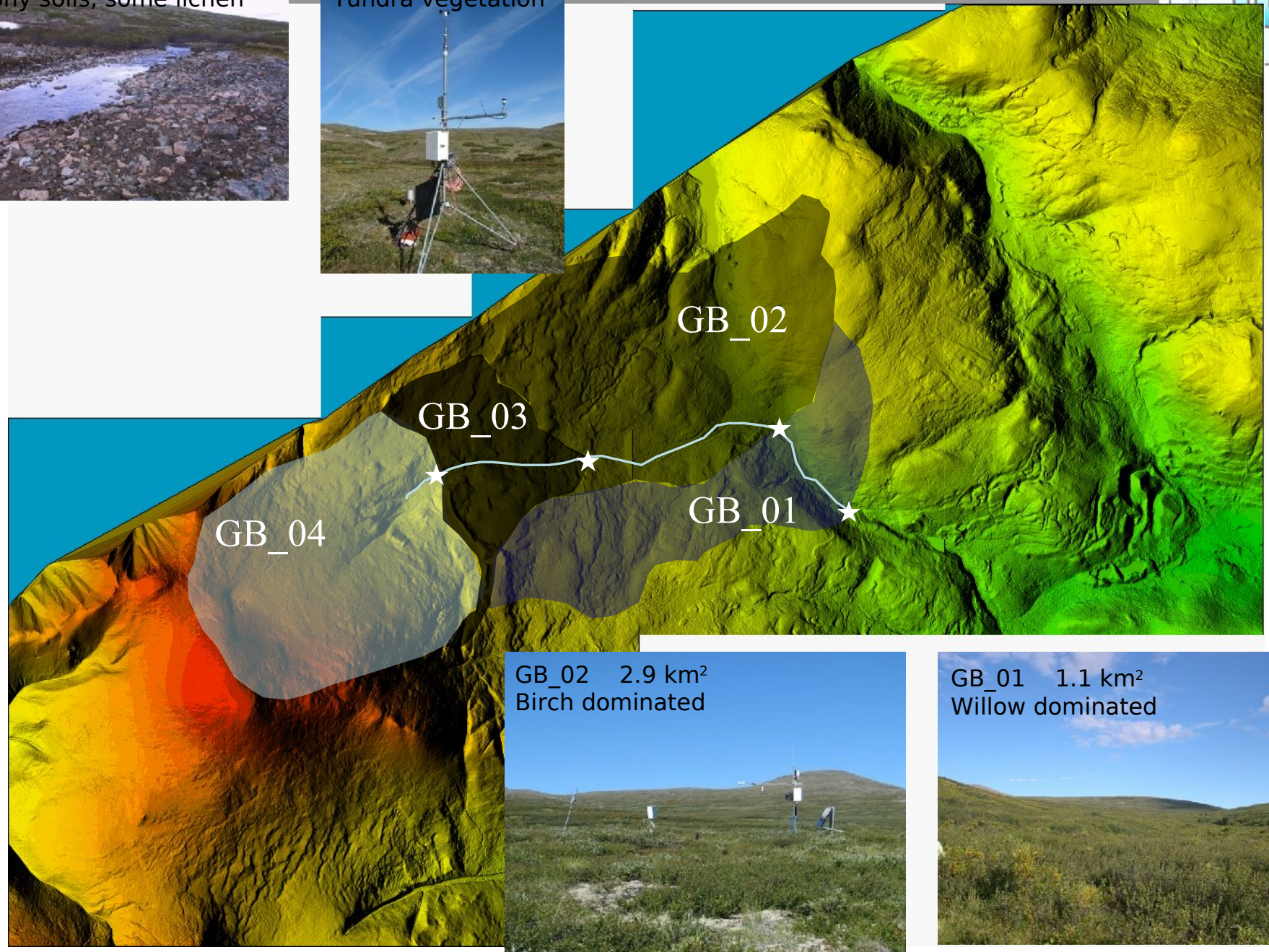
Area:  
Approx. 200 km<sup>2</sup>

Elevation Range:  
800 to 2250 m a.s.l.  
(3 ecozones)

Mean Annual Precipitation:  
300 to 400 mm (40% snow)

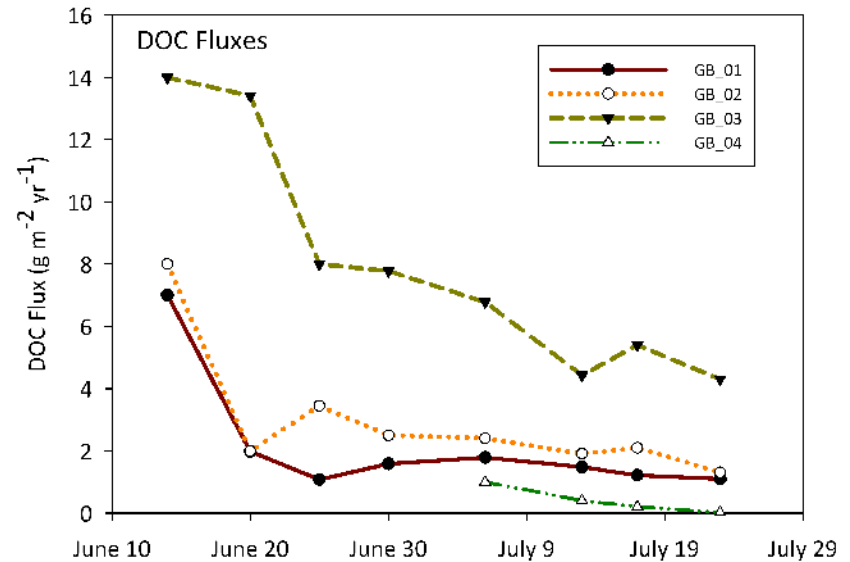
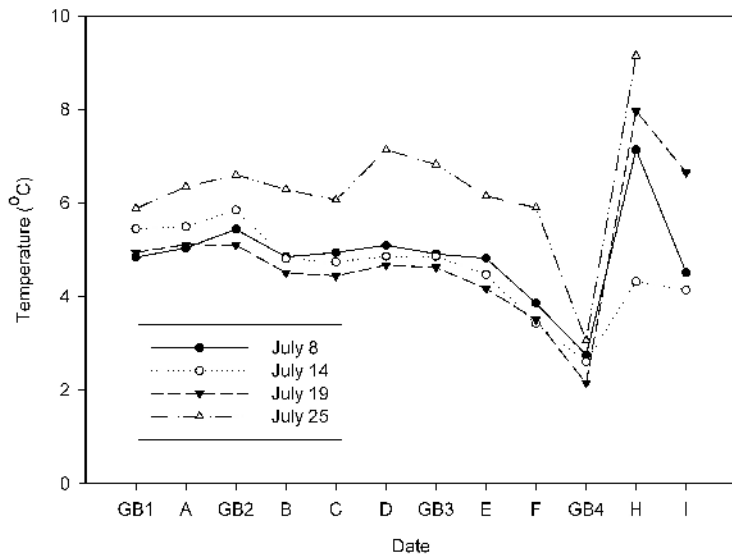
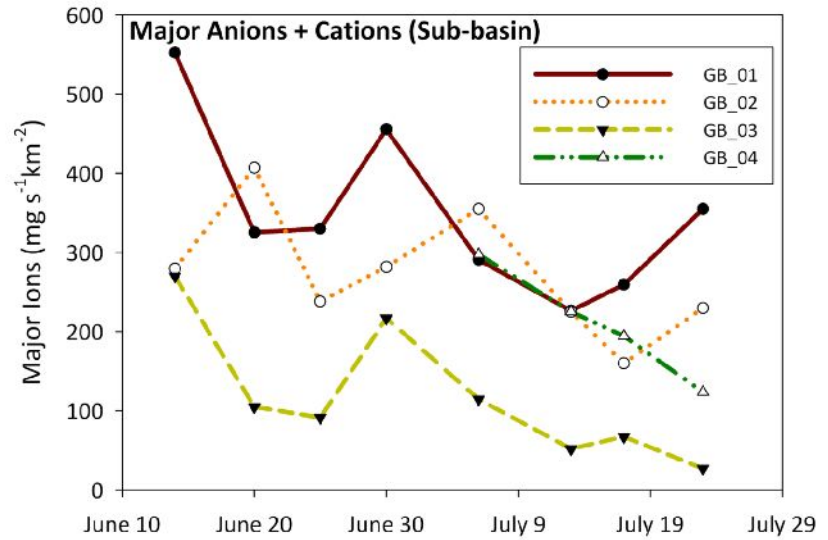
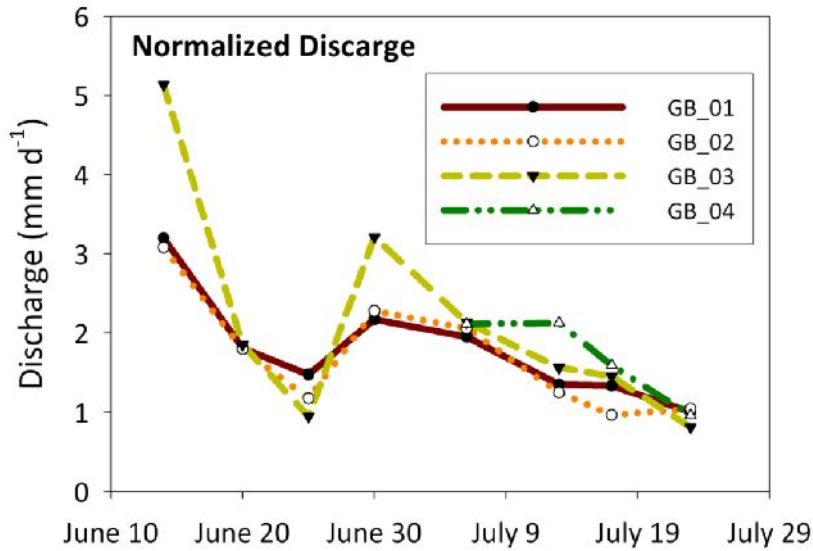
Mean Annual Temperature:  
-3 °C







# Data - Simple Hydrochemistry





# Last Year's summary

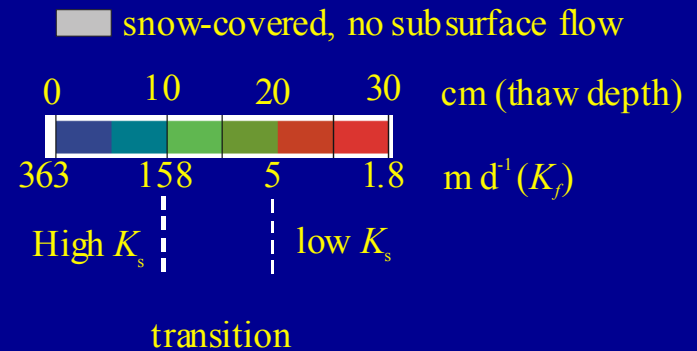
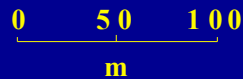
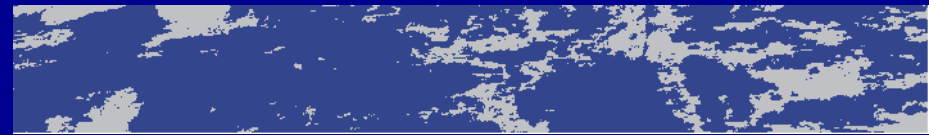
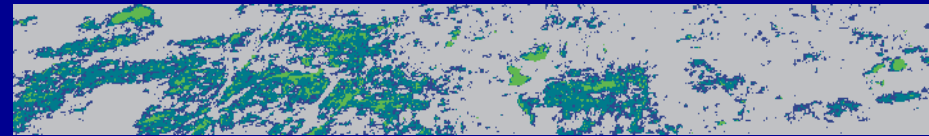


- All HRUs contribute water to the stream in approximately equal volume.
- Much greater deep groundwater flow than previously reported or anticipated.
- Work ongoing to assess seasonal dominance of HRUs (logistics).
- Role of channel ice/snow to be investigated



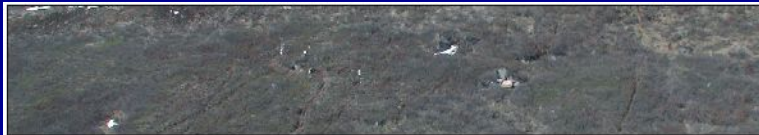


# Hillslope Runoff - Energy Dynamics





# Hillslope Runoff – Energy Dynamics



0 50 100  
m

## HYDROLOGICAL PROCESSES

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## Towards an energy-based runoff generation theory for tundra landscapes

William L. Quinton<sup>1\*</sup> and Sean K. Carey<sup>2</sup>

<sup>1</sup> Cold Regions Research Centre, Wilfrid Laurier University, Waterloo, N2L 3C5, Canada

<sup>2</sup> Geography and Environmental Studies, Carleton University, Ottawa, K1S 5B6, Canada

\*Correspondence to: William L. Quinton, Cold Regions Research Centre, Wilfrid Laurier University, Waterloo, N2L 3C5, Canada. E-mail: wquinton@wlu.ca

### Abstract

Runoff hydrology has a large historical context concerned with the mechanisms and pathways of how water is transferred to the stream network. Despite this, there has been relatively little application of runoff generation theory to cold regions, particularly the expansive treeless environments where tundra vegetation, permafrost, and organic soils predominate. Here, the hydrological cycle is heavily influenced by 1) snow storage and release, 2) permafrost and frozen ground that restricts drainage, and 3) the water holding capacity of organic soils. While previous research has adapted temperate runoff generation concepts such as variable source area, transmissivity feedback, and fill-and-spill, there has been no runoff generation concept developed explicitly for tundra environments. Here, we propose an energy-based framework for delineating runoff contributing areas for tundra environments. Aerodynamic energy and roughness height control the end-of-winter snow water equivalent, which varies orders of magnitude across the landscape. Radiant energy in turn controls snowmelt and ground thaw rates. The combined spatial pattern of aerodynamic and radiant energy control flow pathways and the runoff contributing areas of the catchment, which are persistent

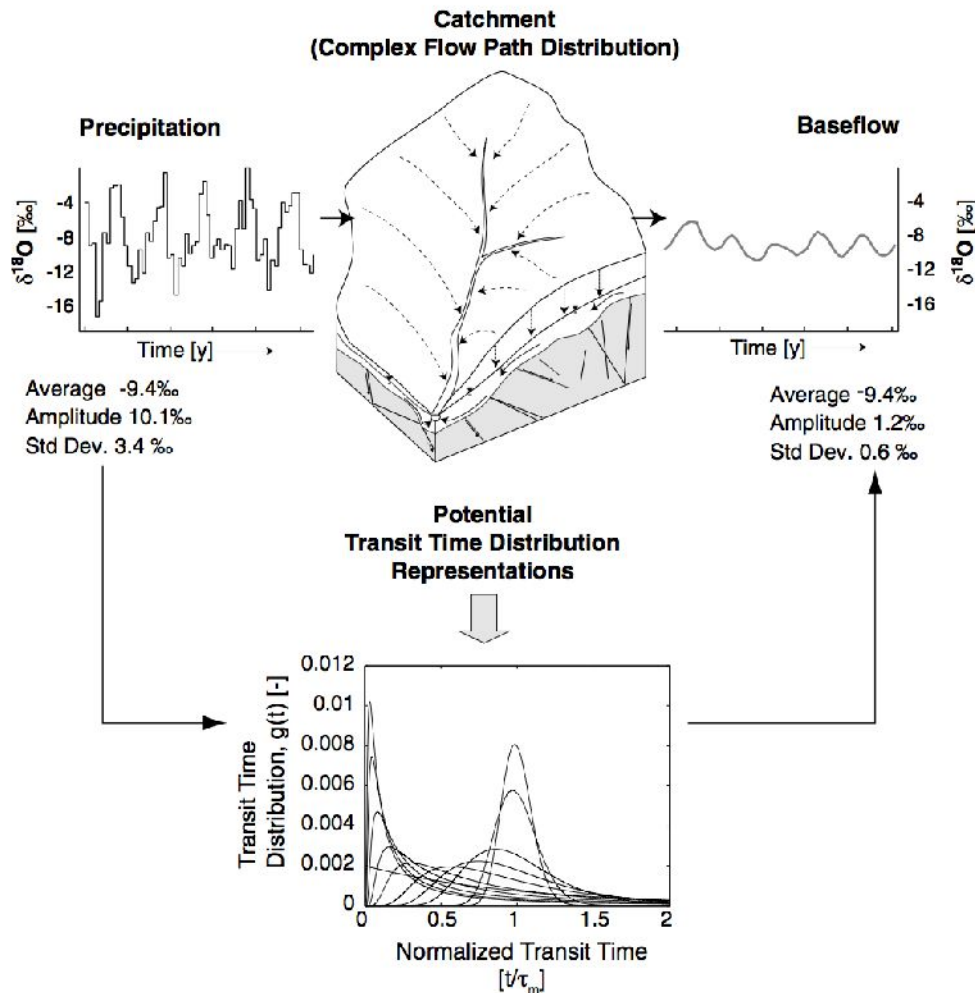




# Transit/Residence Time Distribution



Residence Time: time (since entry) that a water molecule has spent inside a flow system





# Residence Time Assumptions



$$\delta_{out}(t) = \int_0^{\infty} g(\tau) \delta_{in}(t - \tau) d\tau$$

Convolution integral

$$\delta_{out}(t) = \frac{\int_0^{\infty} g(\tau) w(t - \tau) \delta_{in}(t - \tau) d\tau}{\int_0^{\infty} g(\tau) w(t - \tau) d\tau}$$

Weighed recharge (a must!)

Model	Residence Time Distribution $g(\tau)$	Parameters	Mean Residence Time <sup>a</sup>
Exponential <sup>b</sup>	$\tau_m^{-1} \exp(-\tau/\tau_m)$	$\tau_m$	$\tau_m$
Exponential-piston flow <sup>b</sup>	$\left(\frac{\tau_m}{\eta}\right)^{-1} \exp\left(-\frac{\eta\tau}{\tau_m} + \eta - 1\right)$ for $\tau \geq \tau_m(1 - \eta^{-1})$ 0 for $\tau < \tau_m(1 - \eta^{-1})$	$\tau_m, \eta$	$\tau_m$
Dispersion <sup>b</sup>	$\left(\frac{4\pi D_p \tau}{\tau_m}\right)^{-1/2} \tau^{-1} \times \exp\left[-\left(1 - \frac{\tau}{\tau_m}\right)^2 \left(\frac{\tau_m}{4D_p \tau}\right)\right]$	$\tau_m, D_p^c$	$\tau_m$
Gamma <sup>d</sup>	$\frac{\tau^{\alpha-1}}{\beta^\alpha \Gamma(\alpha)} \exp(-\tau/\beta)$	$\alpha, \beta$	$\alpha\beta$
Two parallel linear reservoirs <sup>e</sup>	$\frac{\phi}{\tau_f} \exp\left(-\frac{\tau}{\tau_f}\right) + \frac{1-\phi}{\tau_s} \exp\left(-\frac{\tau}{\tau_s}\right)$	$\tau_f, \tau_s, \phi$	—
Power law <sup>f</sup>	$\frac{\tau^k}{\Gamma(1-k)}$	$k$	—



$$\delta_{out}(t) = \int_0^{\infty} g(\tau) \delta_{in}(t - \tau) d\tau$$

Convolution integral

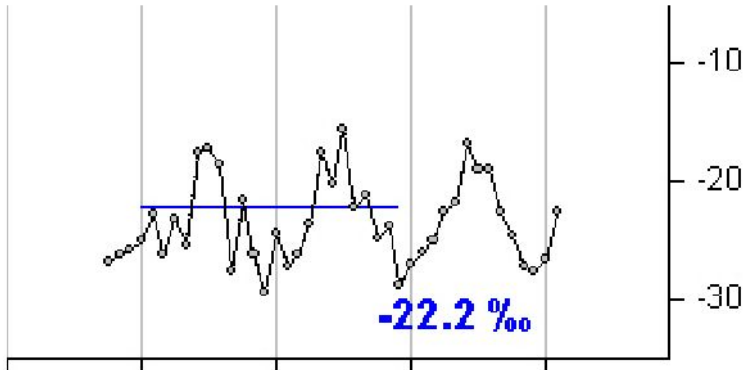
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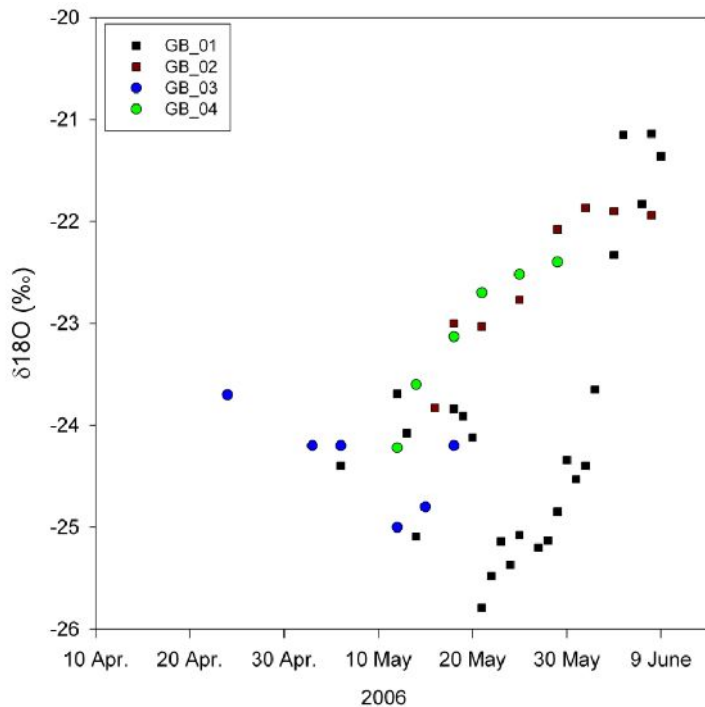
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Power law <sup>f</sup>	$\frac{\tau^k}{\Gamma(1-k)}$	$k$	—



# Inputs – tough with lots of assumptions



- Use Whitehorse  $\delta^{18}\text{O}$  curve for post-melt period
- No input after October to melt
- Observed meltwater  $\delta^{18}\text{O}$  and volume
- “flow weighted”

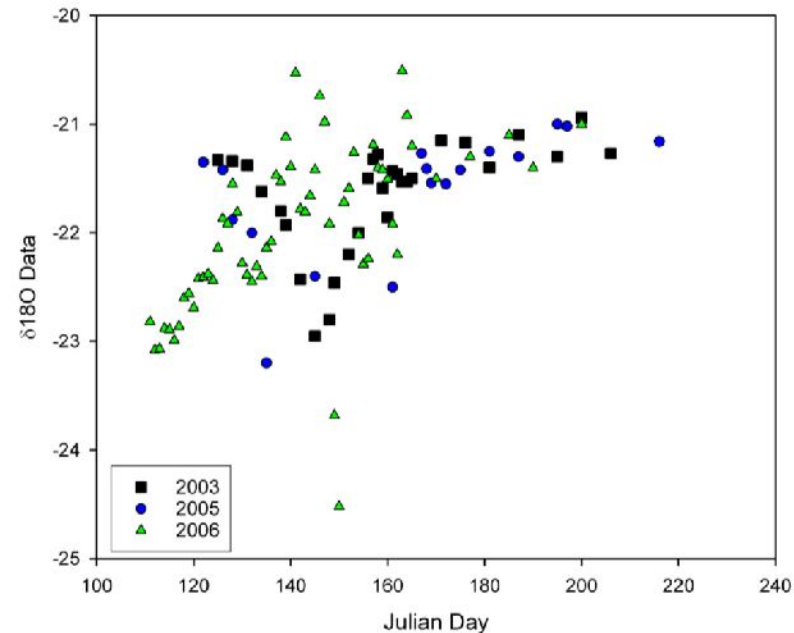




# Outputs - messy!

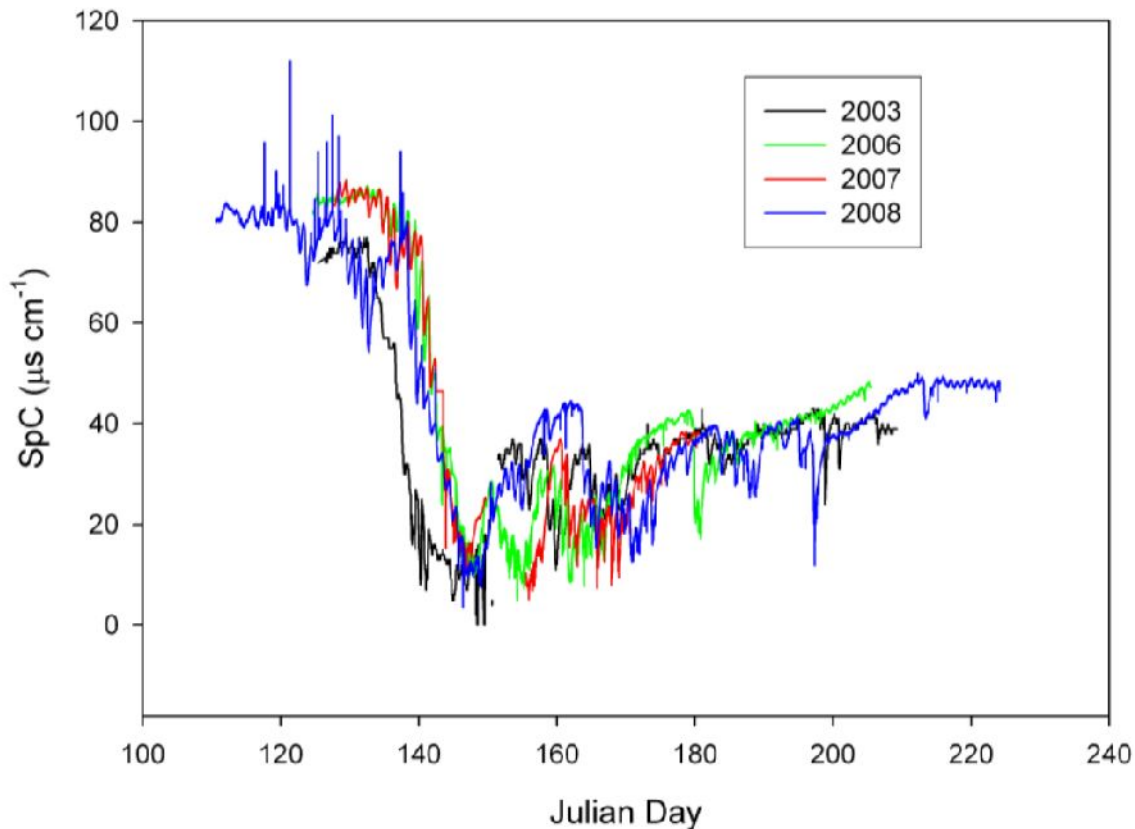


- Lag times need to be adjusted if considering rainfall versus snowmelt (may want to consider only melt signatures or rain/melt separately)
- Parameter converge does occur (GLUE), yet N-S goodness of fit “mediocre”  $\sim 0.6$  to  $0.7$
- Mean Residence Times fast compared with temperate catchments ( $< 2$  months) - the melt signature strongly influences the result.





- Development of a SpC budget as a way forward (stronger and cleaner signal)
- SpC, while not conservative, has a strongly weighted snowmelt signature
- RTD can be further assessed using runoff models at event-scale and tracer data
- Off to Aberdeen in February for advice.



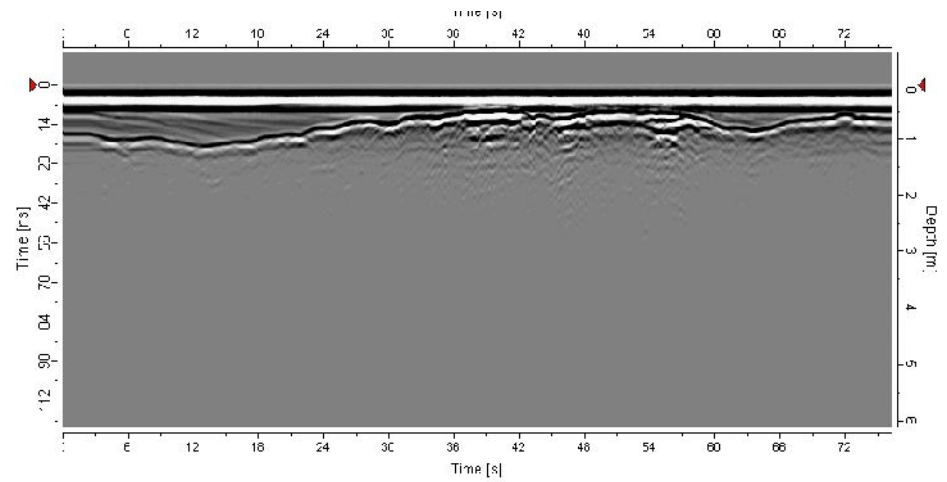


# The Role of Channel Ice and Snow



- What is the role of icing and channel ice?











- Evaluate several commonly used infiltration algorithms using field measurements at several organic covered permafrost sites
- Identify the key parameters/processes in infiltration simulations at organic covered permafrost soil.
- Provide guidelines for the implementation of appropriate infiltration algorithms/parameters in hydrological and land surface models





# Tested ( ) Infiltration Algorithms



Empirical  
&  
analytical



Gray et al. (1985) SWE based empirical relation

$$INF = \rho(1 - S_I)SWE^{0.085}$$

Zhao and Gray (1999) parametric relation

$$INF = CS^{0.95}(1 - S_I)^{1.75} \left( \frac{273.15 - T_L}{273.15} \right)^{-0.5} t^{0.45}$$

Green\_Ampt (1911) and various modifications

$$INF_r = K_s \left[ 1 + \frac{(\theta_0 - \theta_i)\psi_w}{F} \right]$$

Numerical



Numerical solvers of Richard's equation or coupled heat and water transfer equations with water flux as surface boundary

e.g. HYDRUS1D (Šimůnek et al., 2005), HAWTS (Zhao et al., 1997) etc.

Mixed  
(analytical+  
numerical)



ARHYTHM Instantaneous Infiltration model (Zhang et al., 2000) (TopoFlow)

SHAW infiltration - modified Green\_Ampt Approach for Muti-layered soil (Flerchinger and Saxton, 1989)



Ground surface temperature ( $T_0$ )

- Observed surface or near surface temperature

Snow-melt ( $M_{sn}$ ) and rainfall ( $R$ )

- Scotty Creek: daily SWE observation and tipping-bucket rain gauge
- Wolf Creek: daily snow depth with in situ snow density samples and tipping-bucket rain gauge

Evapotranspiration ( $ET$ ) --Site calibrated Priestley- Taylor (1972)

Infiltration ( $\Delta SW_{liq} / \Delta SW_{total}$  : liquid / total soil water changes;  
 $SW_{melt}$  : soil ice melt)

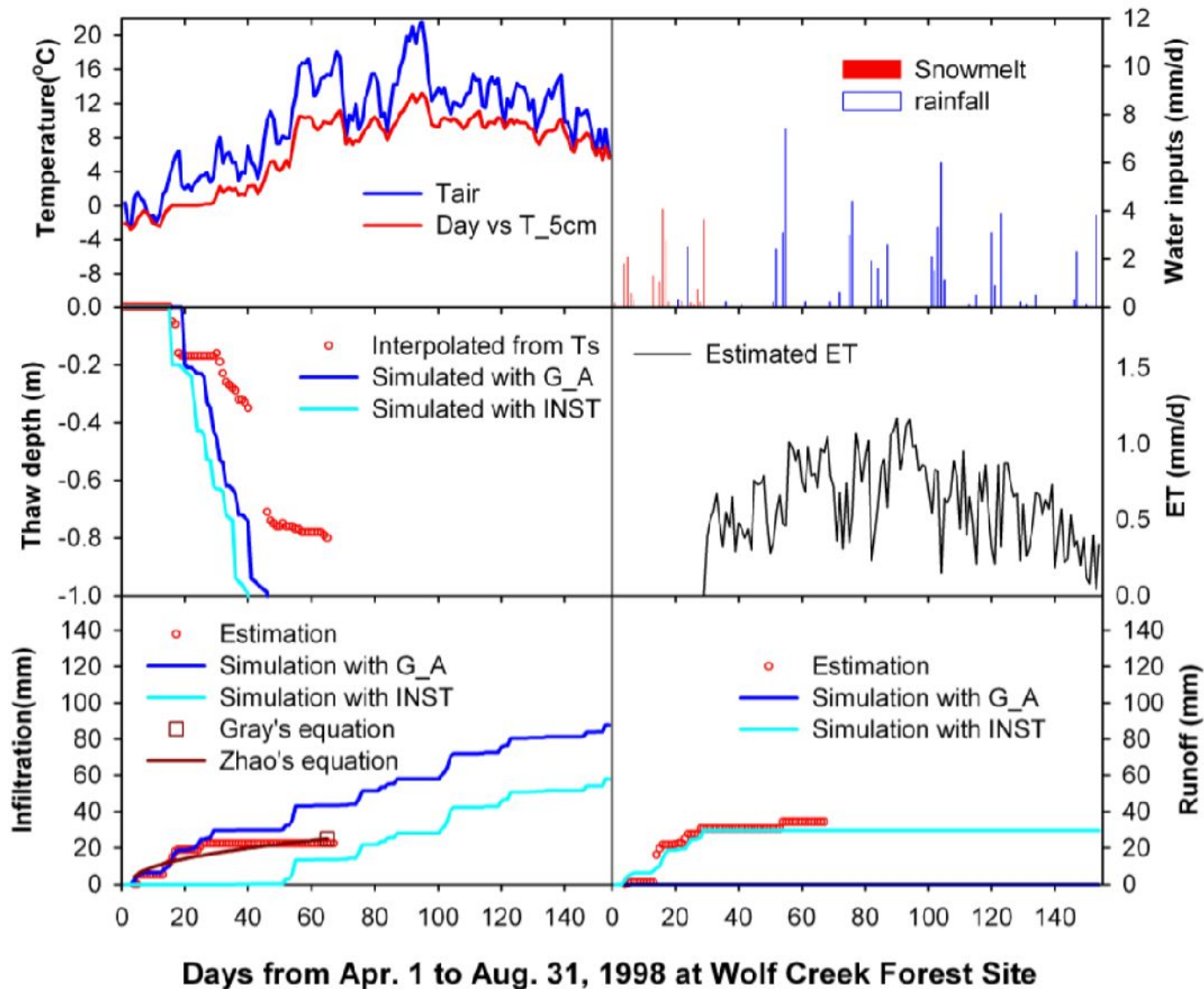
- Scotty Creek:  $INF_{est} = \Delta SW_{liq} - SW_{melt} + ET$  (if positive)
- Wolf Creek:  $INF_{est} = \Delta SW_{total} + ET$  (if positive)

Runoff

- Scotty Creek:  $Runoff_{est} = R + M_{sn} + SW_{melt} - \Delta SW_{liq} - ET$  (if positive)
- Wolf Creek:  $Runoff_{est} = R + M_{sn} - \Delta SW_{total} - ET$  (if positive)



# Wolf Creek Simulations: control variables, thaw depth, infiltration and runoff



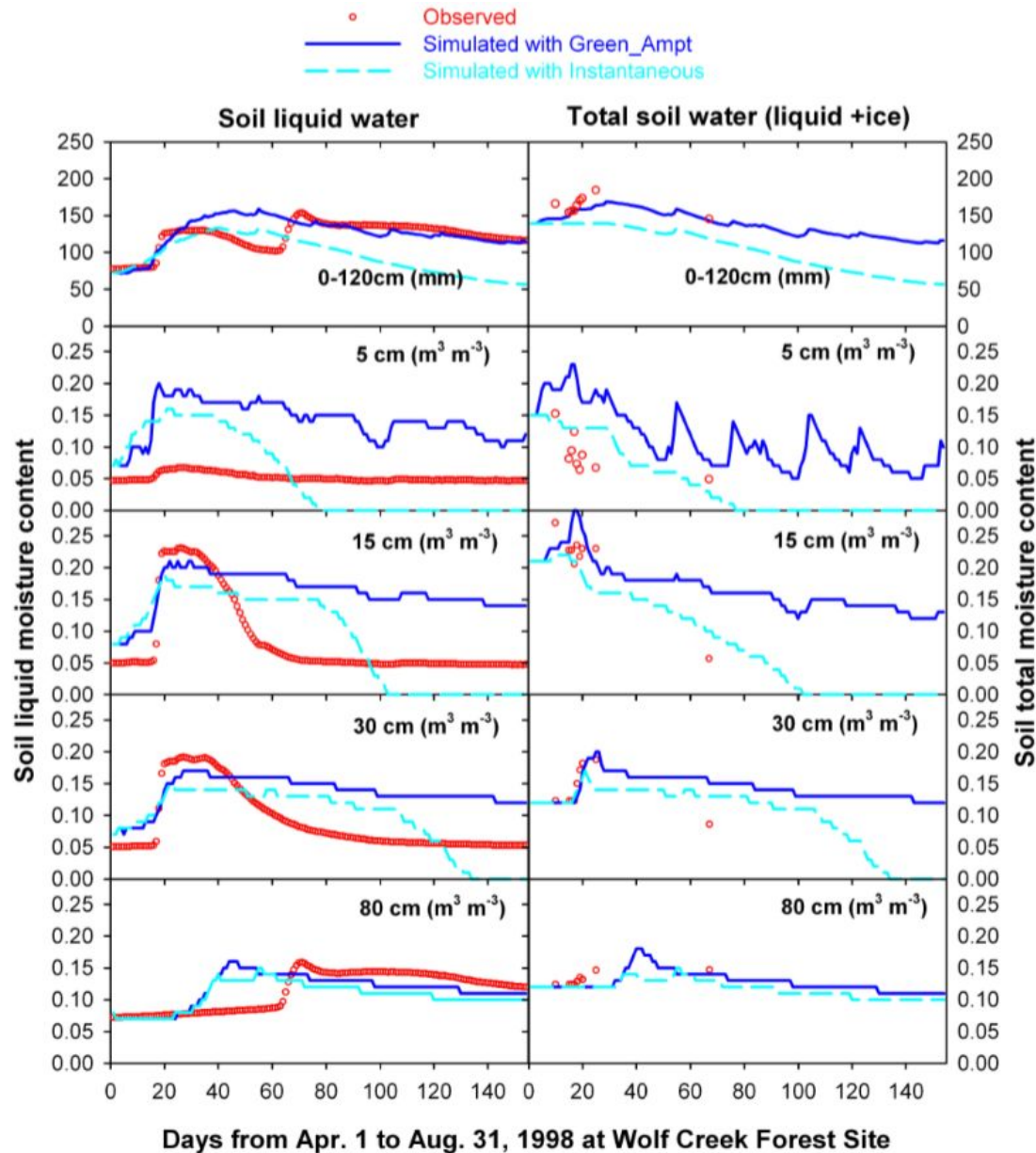


# Wolf Creek: Soil Moisture Simulations and Observations



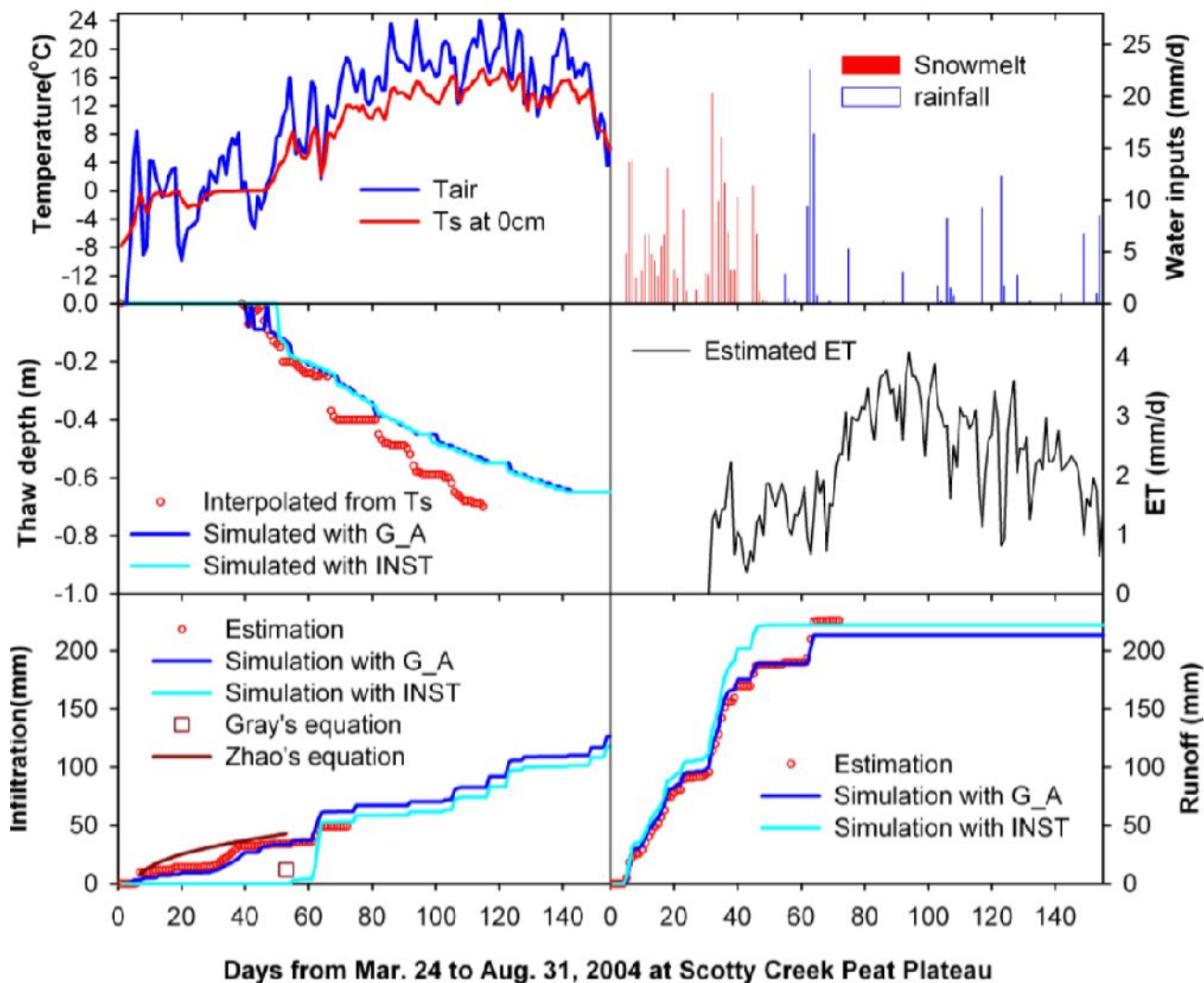
- Liquid: TDR

- Total: Gamma





# Scotty Creek Simulations: control variables, thaw depth, infiltration and runoff



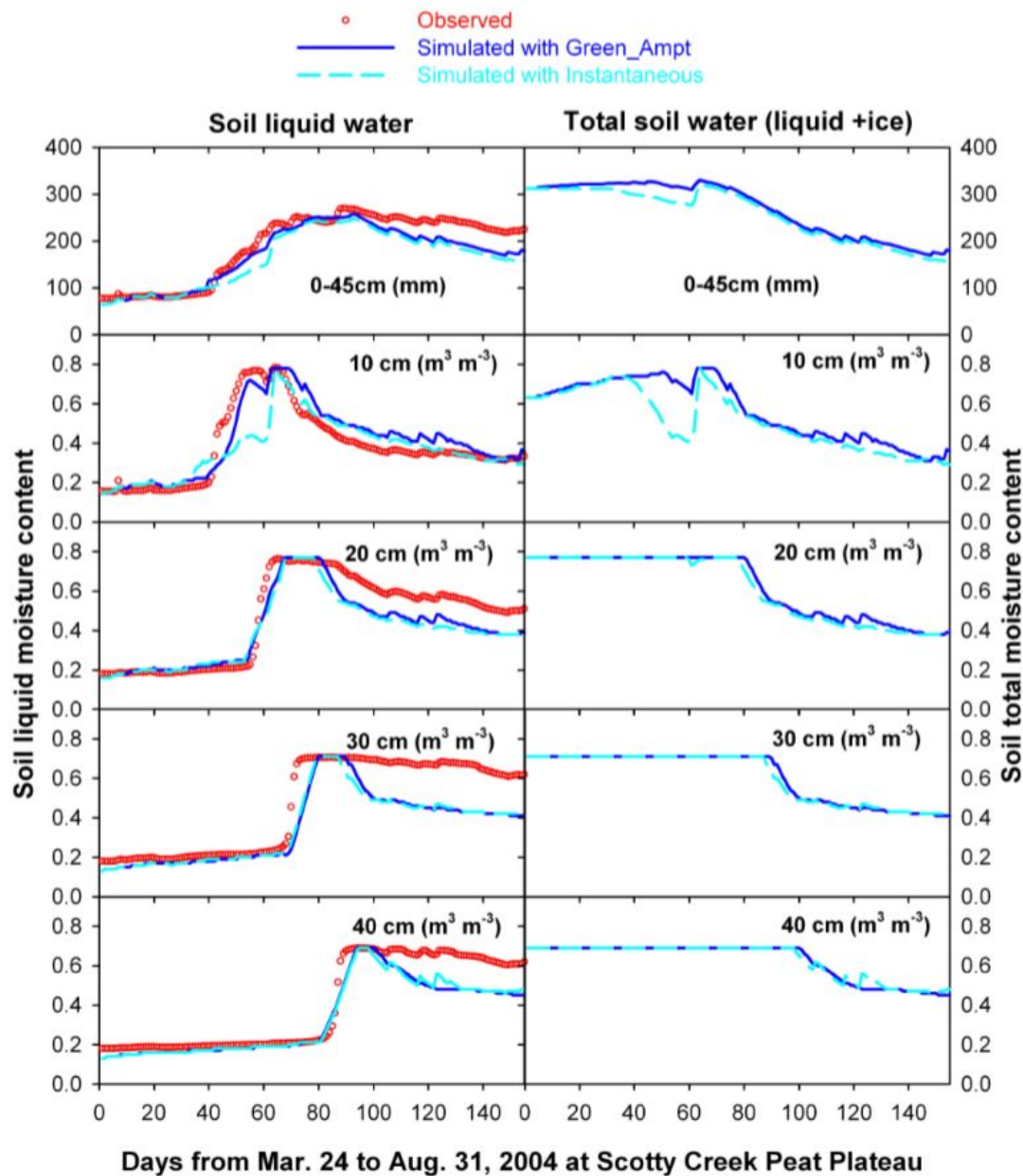


# Scotty Creek: Soil Moisture Simulations and Observations



- Liquid: TDR

- Total: None







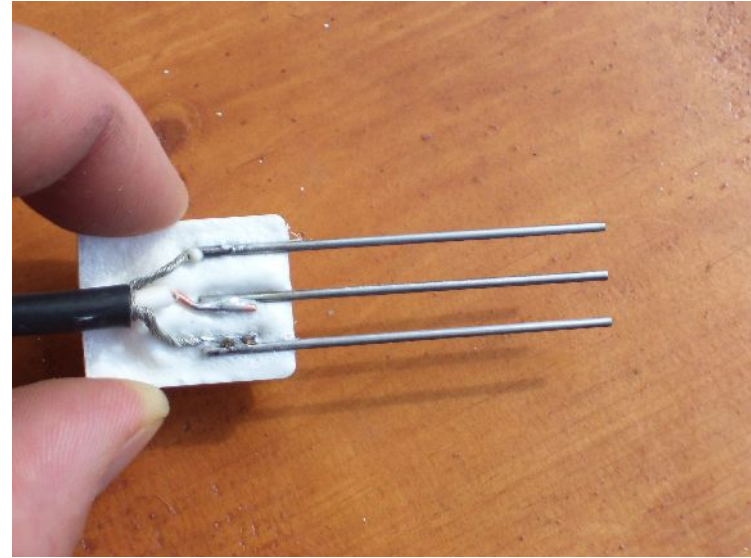
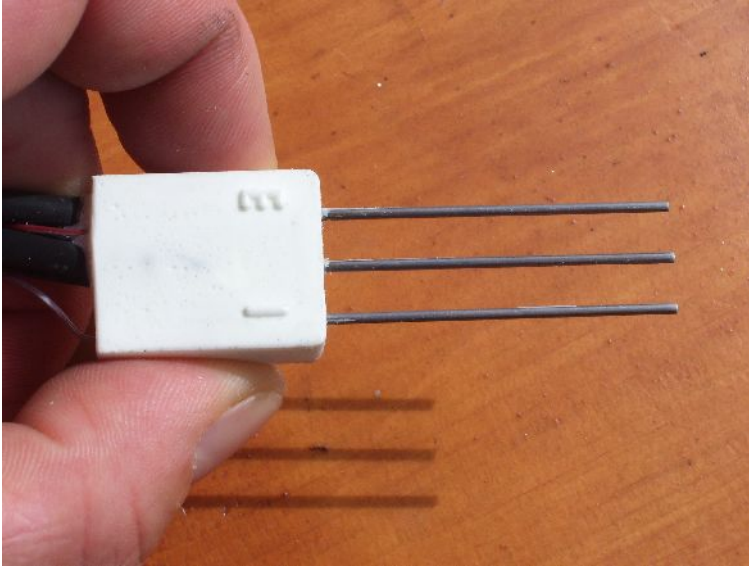
# Preliminary results and ongoing works



- ▶ Gray's empirical estimation gave an acceptable estimation for cumulative end-season snow-melt infiltration at Wolf Creek, but largely underestimated the infiltration at Scotty Creek, due to the near saturated soil condition.
- ▶ The parametric method (Zhao et al.) worked at both sites in terms of cumulative end-season snow-melt infiltration, however its power-shaped curve did not follow the actual daily infiltration course.
- Pure numerical solutions for infiltration problems require very fine time and soil layer resolutions ( $\sim$ minute /  $\sim$ cm), hence very difficult to be applied in field applications.
- ▶ Mixed methods with coupled thermal and water transfer equations have the capacity to simulate the details of infiltration progresses and soil moisture dynamics in. However appropriate algorithms / parameters have to be identified for organic - covered permafrost soils.
- Ongoing works for this study:
  - more expertise is needed in quantifying the inputs/outs from limited observations
  - evaluate the parameterization methods/parameters for thermal and hydraulic properties of those soils at the two sites.
  - Improve the current tested infiltration algorithms for organic -covered permafrost soil.



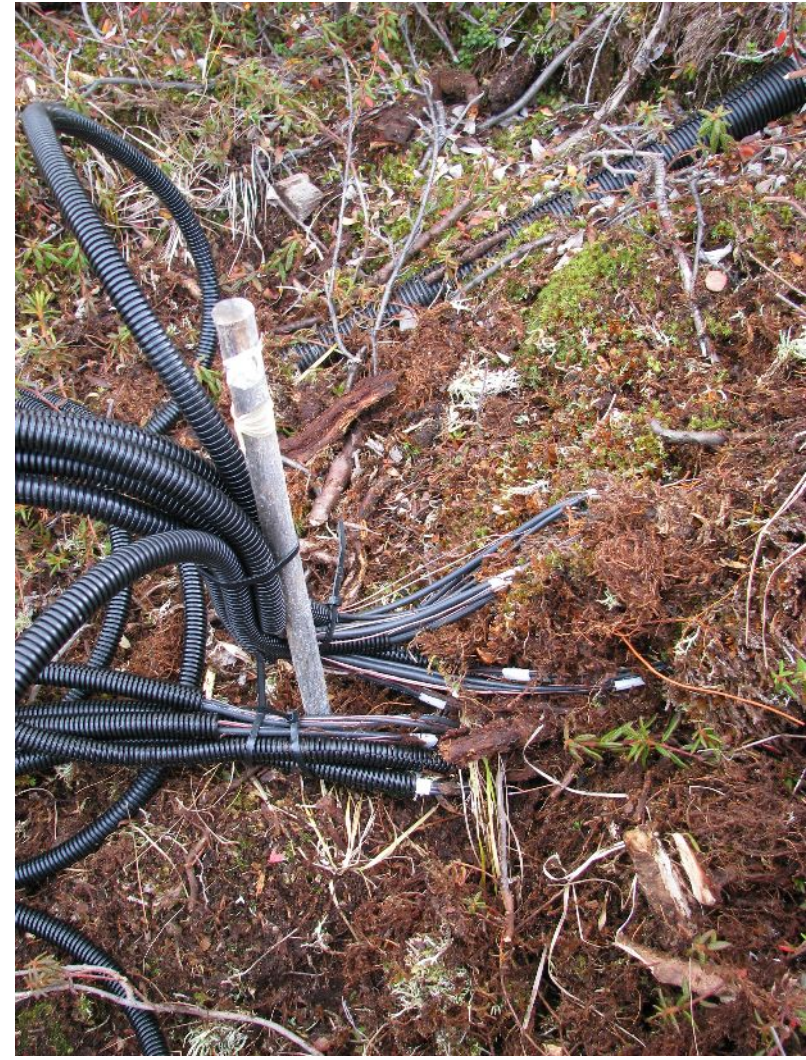
# Multi-Function Heat-Pulse Probes (MFHPP)



- Central probe is a heater
- Outer probes are thermocouples & Reflectometers
- Total water is unknown, liquid is known, all other  $k$  and  $C$  values known
- Inverse procedure allows determination of ice fraction
- Install vertically and horizontally (to measure infiltration similar to sapflow)

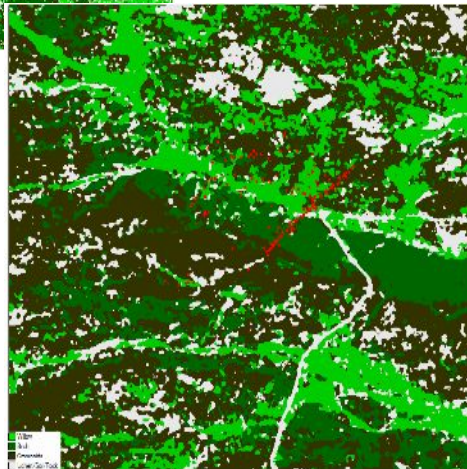
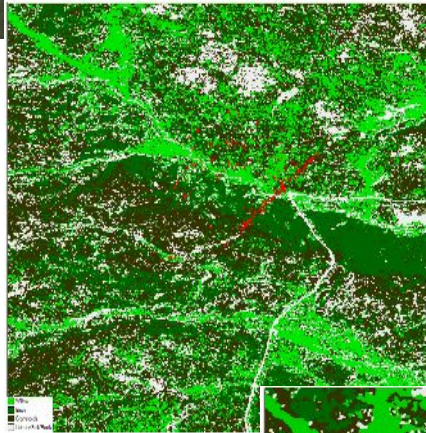


# Multi-Function Heat-Pulse Probes (MFHPP)

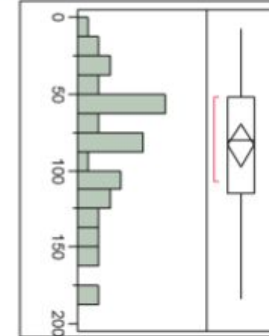




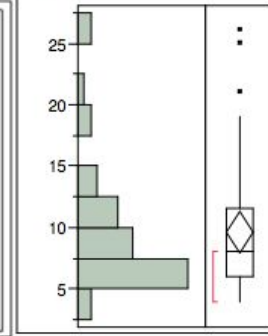
# Image Classification



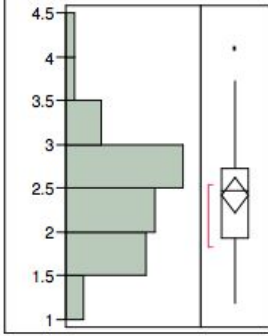
**BIRCH**  
Height (cm)



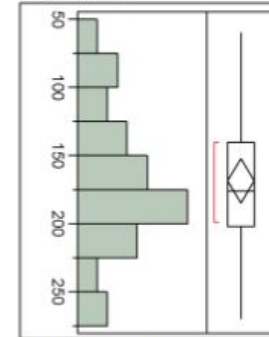
**SMC (%)**



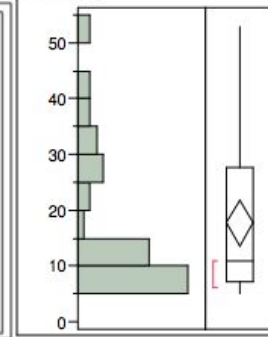
**LAI AVG**



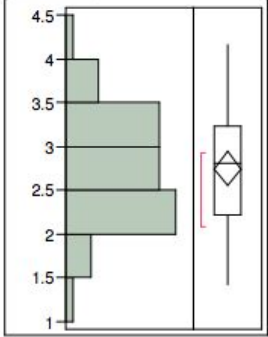
**WILLOW**  
Height (cm)



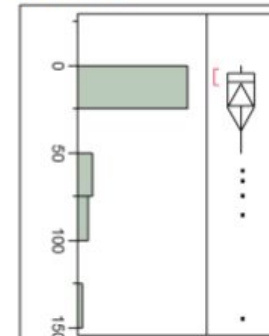
**SMC (%)**



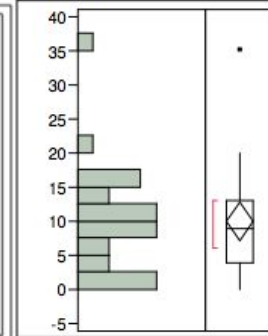
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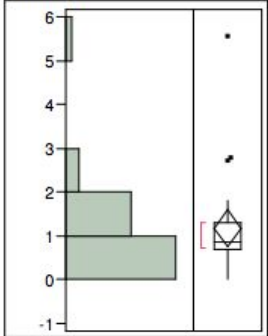
**GRAMINOIDS/ LICHEN**  
Height (cm)



**SMC (%)**



**LAI AVG**





# Ongoing Work

